

Polarization induced renormalization of local interactions in strongly correlated electron systems

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Materials Research
Dresden



TECHNISCHE
UNIVERSITÄT
DRESDEN

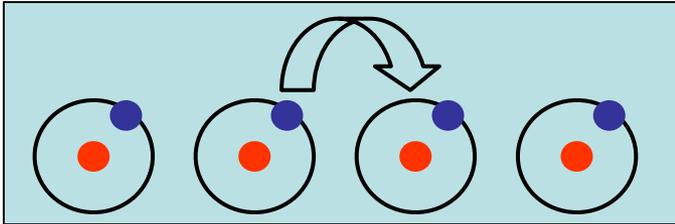
UBC Vancouver
13.04.2016

***Microscopic screening of short-range
Coulomb interactions (e.g. Hubbard U)***

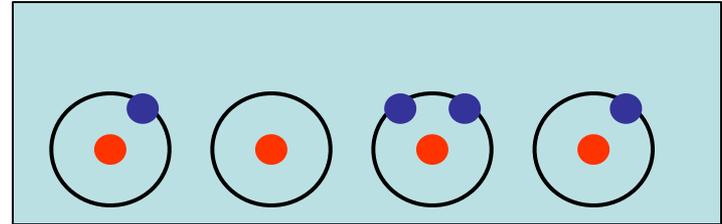
***Resonant Inelastic X-ray Scattering (RIXS)
on Li_2CuO_2
→ phonon screening of CT energy***

Hubbard Hamiltonian

$$H = -t \sum_{\langle ij \rangle, \sigma} (c_{i\sigma}^\dagger c_{j\sigma} + h.c.) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$



Hopping amplitude: t



Coulomb interaction: U

$U = 0$

Bands: Metallic behaviour

$U \gg t$

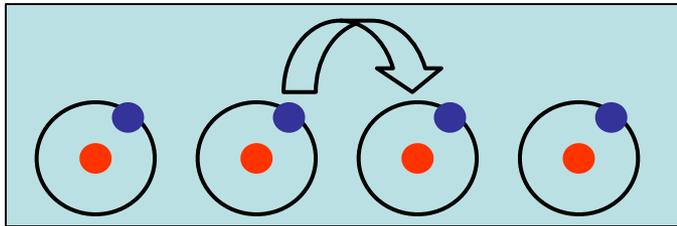
Mott-Hubbard Insulator



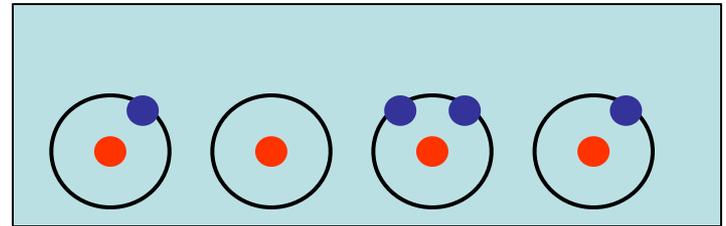
Antiferromagnetism

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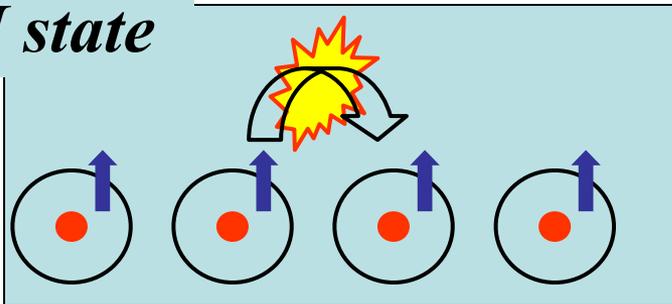
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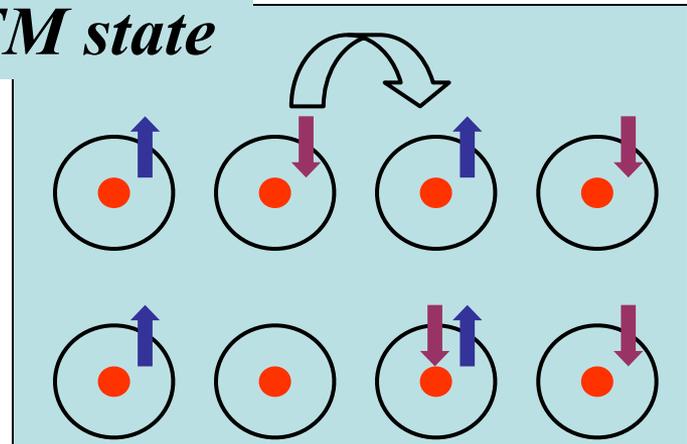
Antiferromagnetism

FM state



$E = 0$

AFM state



$E = -t^2/U$

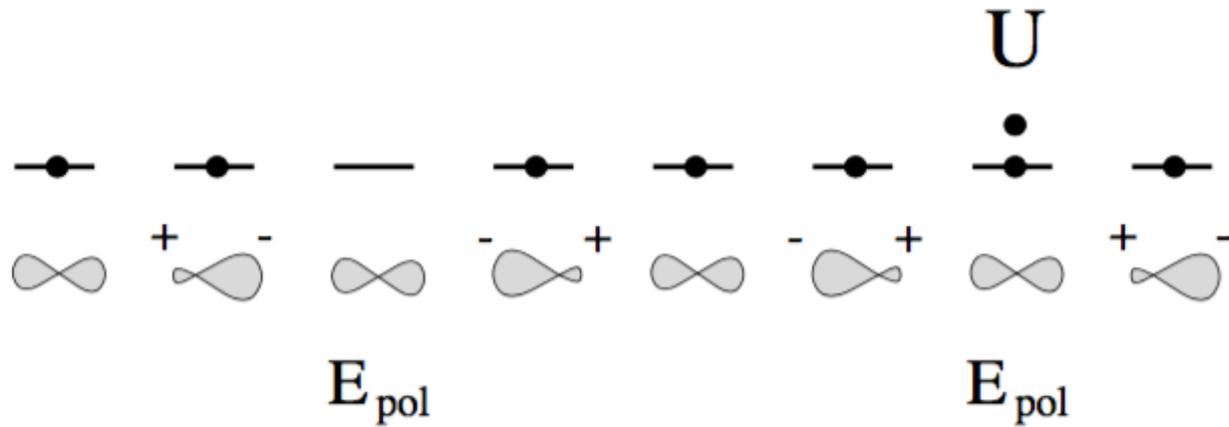
Atomic U versus solid state U

On-site Coulomb Interaction U				
<i>Ion</i>	<i>config</i>	$U_{at}(eV)$	<i>Solid</i>	$U_{sol} (eV)$
Cu	d^9	16.3	CuS	7.0
Ni	d^8	18.0	NiO	7.5
			NiS	5.5
Co	d^7	16.2	CoS ₂	4.2
Fe	d^6	14.7	FeO	7.0
Mn	d^5	20.2	MnO	7.0
C ₆₀		3.4	C ₆₀	1.6

Effective Coulomb interaction for C ₆₀		
<i>Geometry</i>	U^{eff}	V^{eff}
Bulk theory	1.75	0.43
Bulk exp. [20]	1.7 ± 0.2	0.4 ± 0.2
(111) Surface	2.04	0.62
Free Layer	2.49	0.92
Monolayer on Metal	1.00	0.00

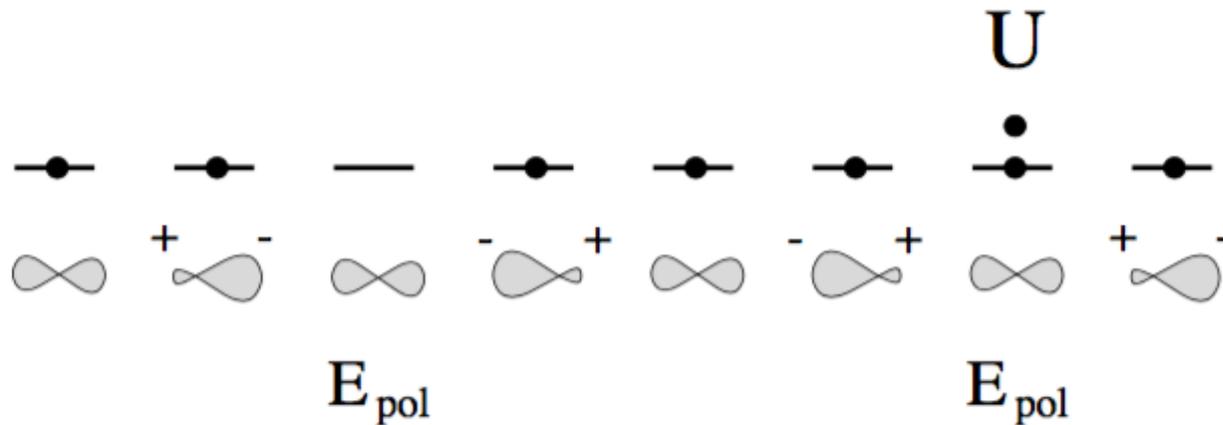
Microscopic origin polarization energy

$$U_{eff} = E_I - E_A - 2Ep.$$



Microscopic origin polarization energy

$$U_{eff} = E_I - E_A - 2E_p.$$



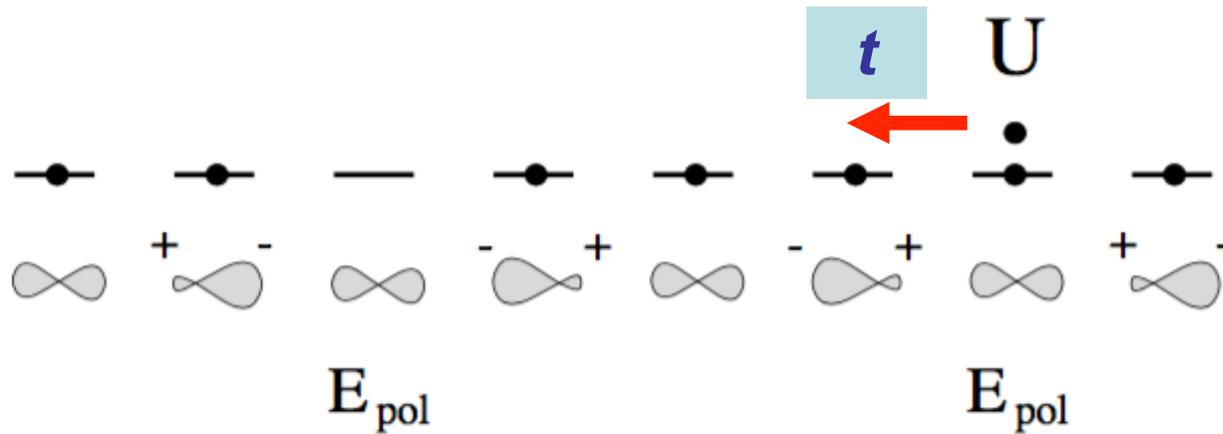
$$\mathbf{p}(\mathbf{r}_i) = \alpha_i^{el} \mathbf{F}(\mathbf{r}_i) \quad \Delta E_i = -\frac{1}{2} \alpha_i^{el} |\mathbf{F}(\mathbf{r}_i)|^2$$

Clausius-Mossotti

$$\frac{\epsilon - 1}{\epsilon + 2} = 4\pi\alpha/3$$

Microscopic origin polarization energy

$$U_{eff} = E_I - E_A - 2E_p.$$



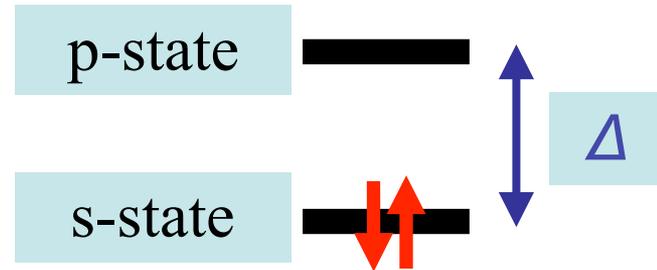
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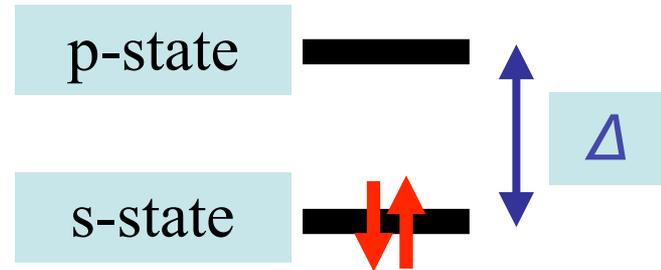
Microscopic polarization

$$H_{\text{pol}}^{1\text{D}} = \frac{e^2}{a^2} |X_{sp}| \sum_i (\hat{n}_{i+1} - \hat{n}_{i-1}) (p_i^\dagger s_i + s_i^\dagger p_i) + \Delta_{sp} p_i^\dagger p_i.$$



Microscopic polarization

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$$E = E_0 - \sum_i \frac{|\langle \phi_i | H_{\text{pol}}^{1\text{D}} | \phi_0 \rangle|^2}{\Delta_{sp}}$$

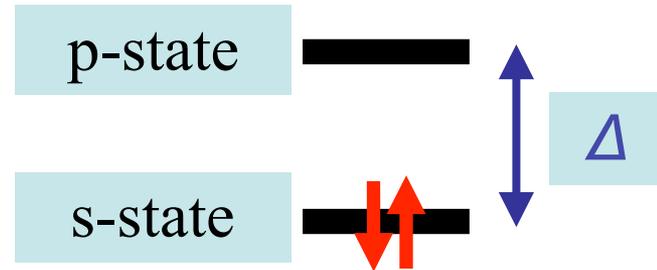
$$= E_0 - \sum_i \frac{(eX_{sp})^2}{\Delta_{sp}} \mathbf{F}_i^2.$$

α

*atomic
polarizability*

Microscopic polarization

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*static
doublon+hole*

$$t/\Delta \rightarrow 0$$

$$E = E_0 - \sum_i \frac{|\langle \phi_i | H_{\text{pol}}^{1\text{D}} | \phi_0 \rangle|^2}{\Delta_{sp}} = E_0 - \sum_i \frac{(eX_{sp})^2}{\Delta_{sp}} \mathbf{F}_i^2.$$

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Polarizability screening of Hubbard U

polarization field:

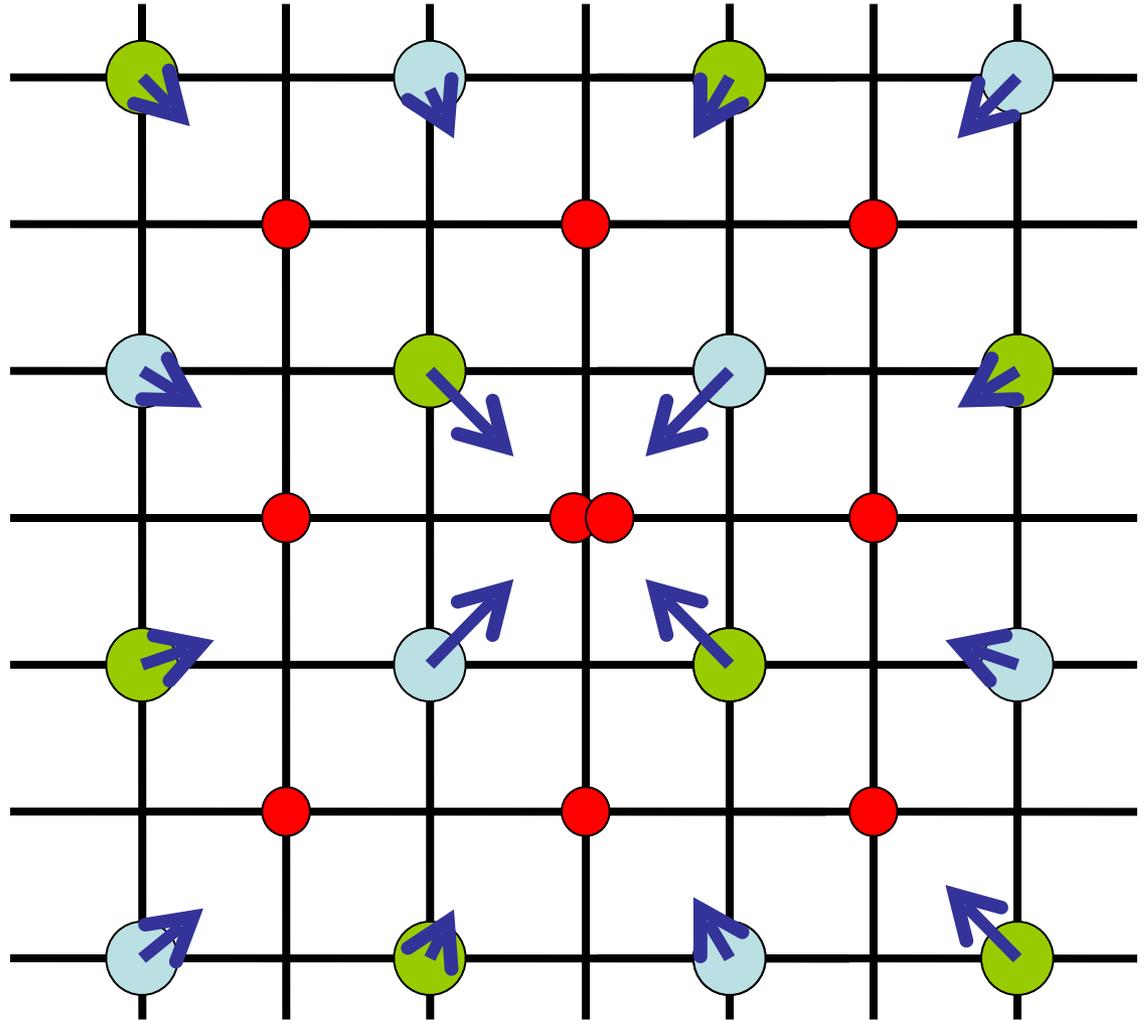
$$\vec{P}_i = \alpha \vec{E}_i$$

atomic
polarizability: α

pol. energy:

$$E_{pol} = \frac{1}{2} \sum_i \vec{E}_i \cdot \vec{P}_i$$

$$\alpha_{\text{oxygen}} \approx 2 \text{ \AA}^3$$



$$U = U_{\text{atomic}} - 2E_{pol}$$

Polarizability screening of Hubbard U

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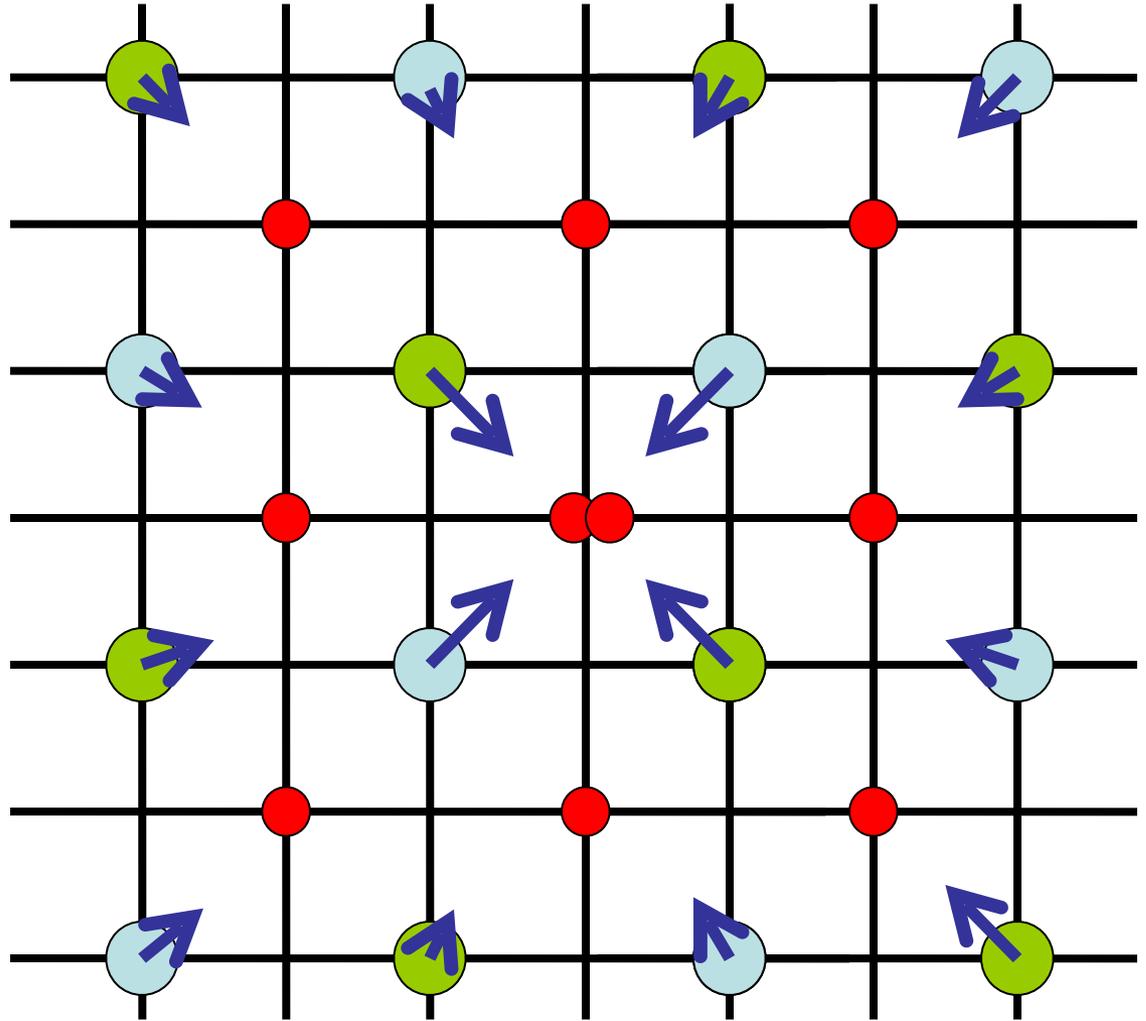
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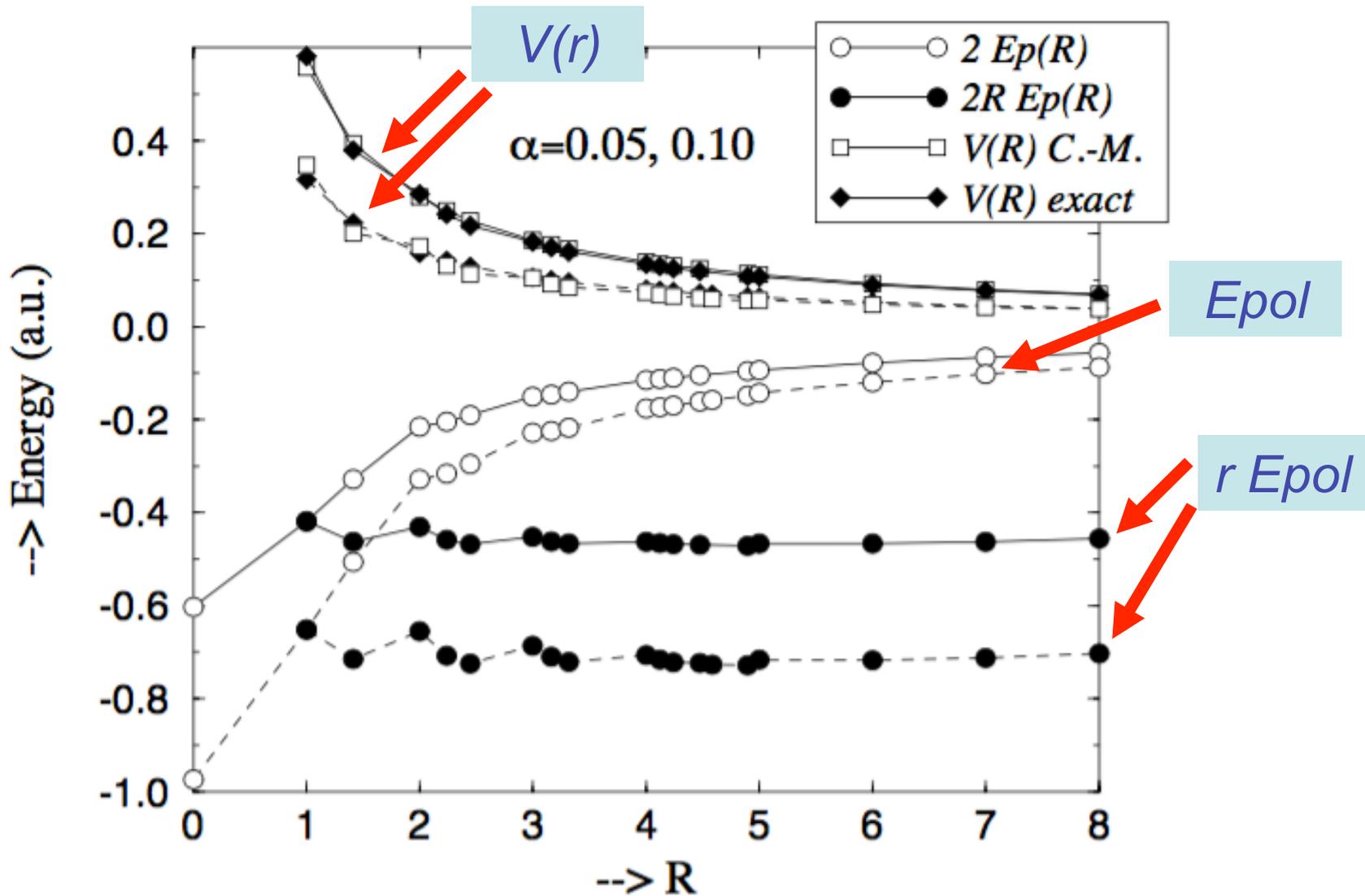
$$\alpha_{\text{oxygen}} \approx 2\text{\AA}^3$$



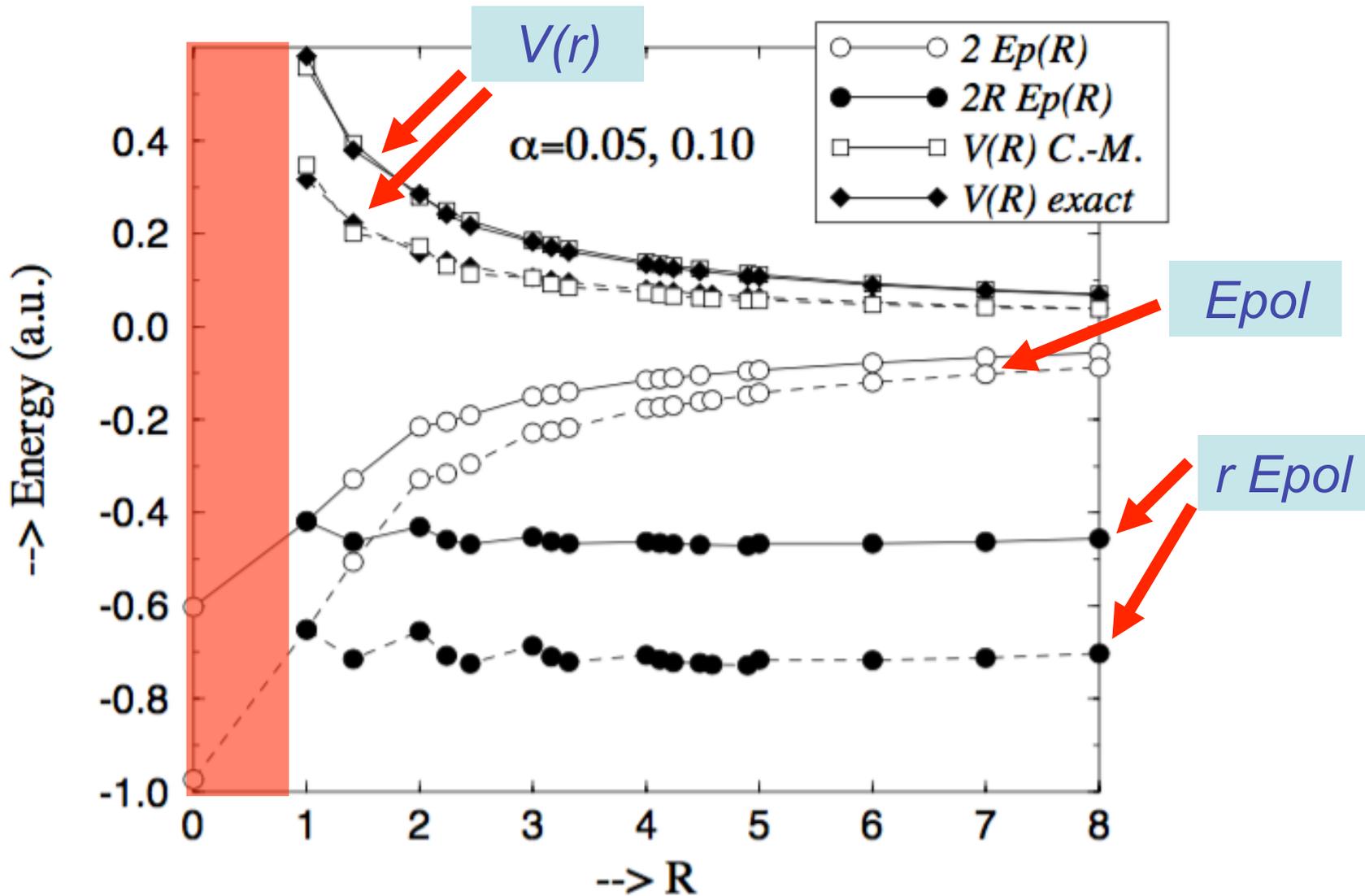
$$U = U_{\text{atomic}} - 2E_{\text{pol}}$$

but does this hold
at large distances?

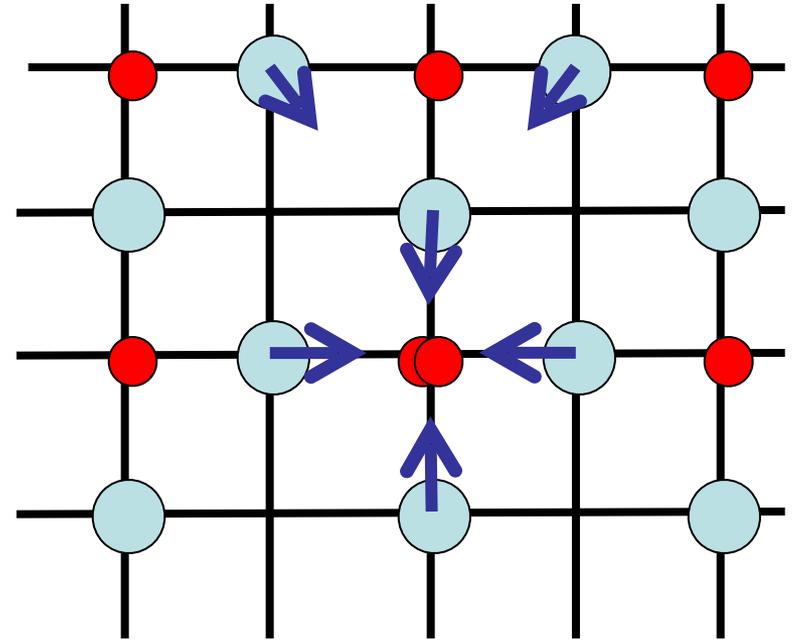
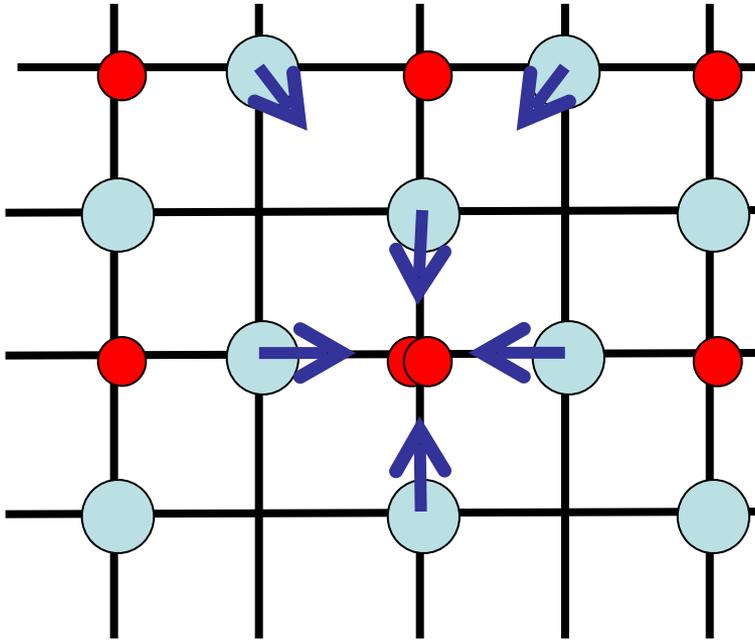
Polarizability versus dielectric screening in 3D



Polarizability versus dielectric screening in 3D



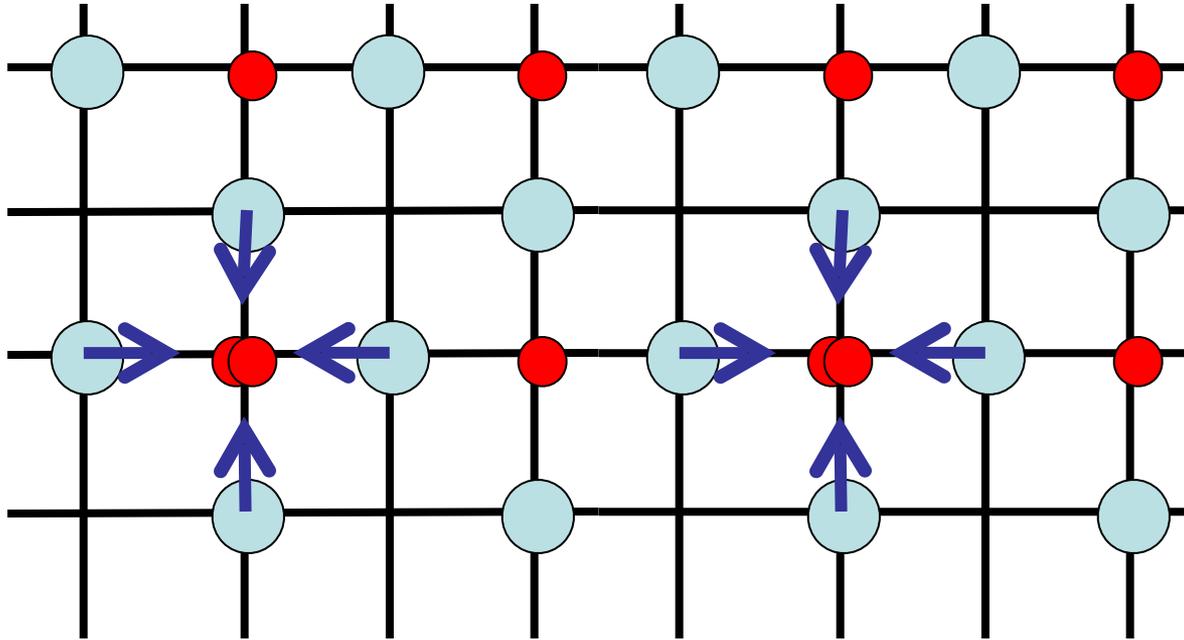
Screening of neighbor V on a 2D CuO_2 lattice



$$\alpha_{\text{oxygen}} \approx 2A^3$$

Cu-O-Cu bond angle 180°

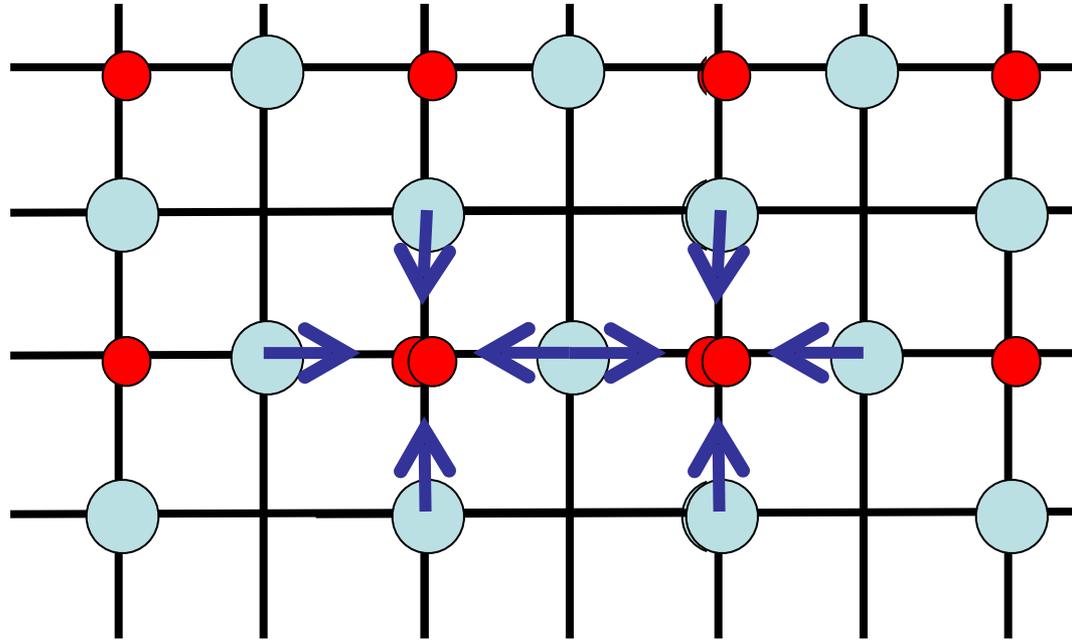
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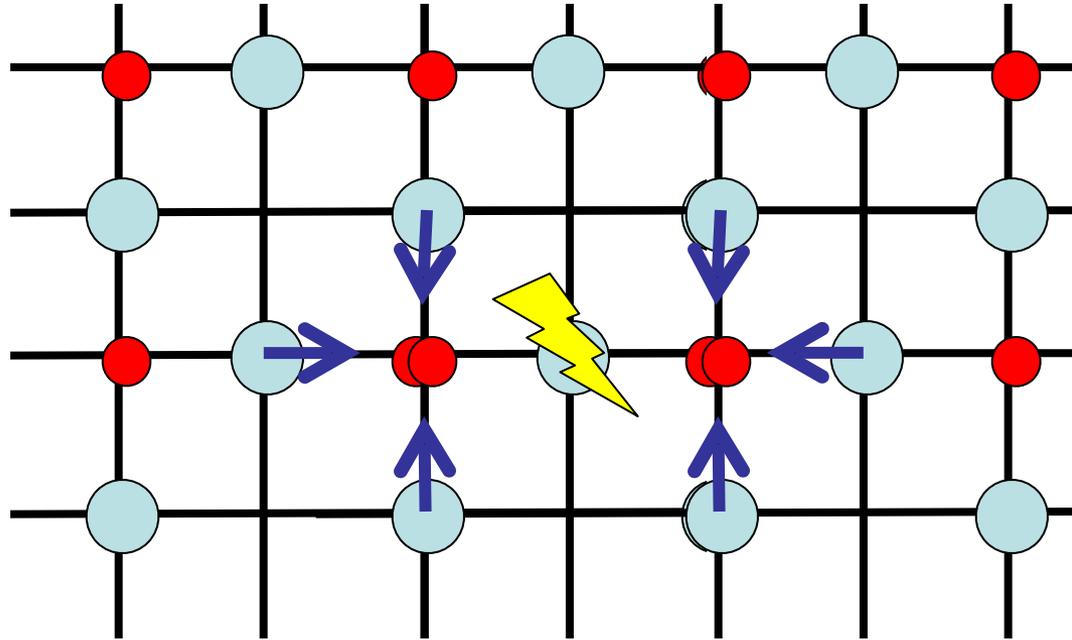
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Screening of neighbor V on a 2D CuO_2 lattice



*polarization partially antiparallel
nearest neighbor V is antiscreened*

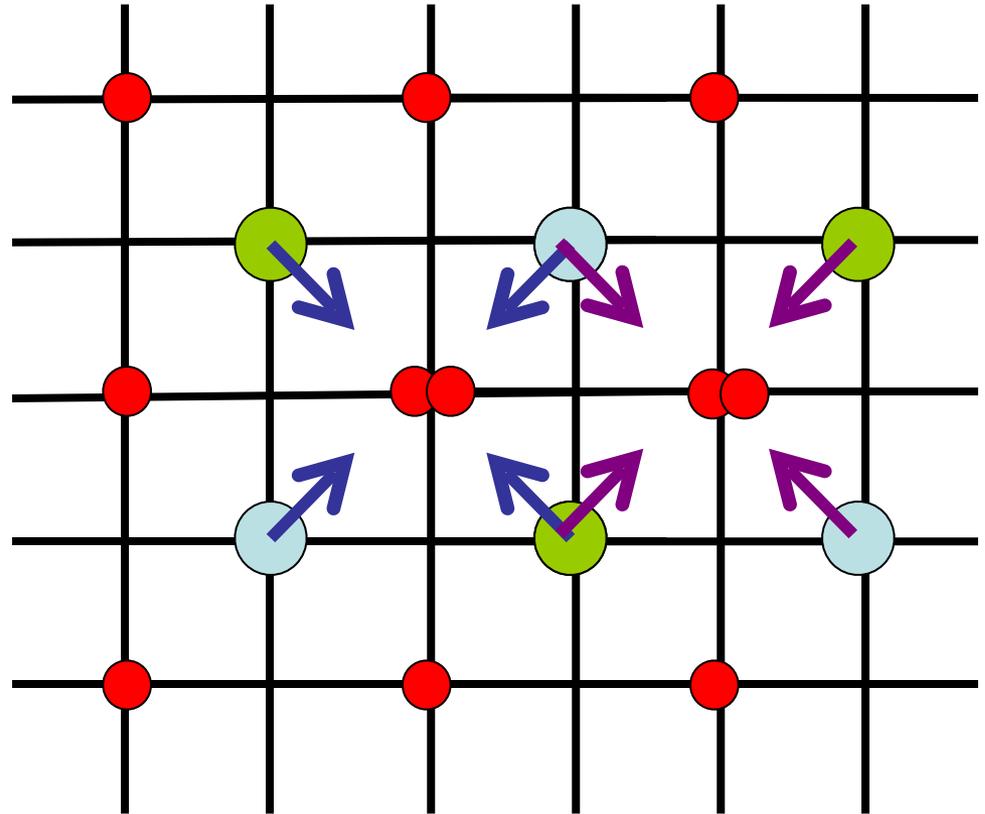
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Screening of neighbor V on 2D cubic lattice

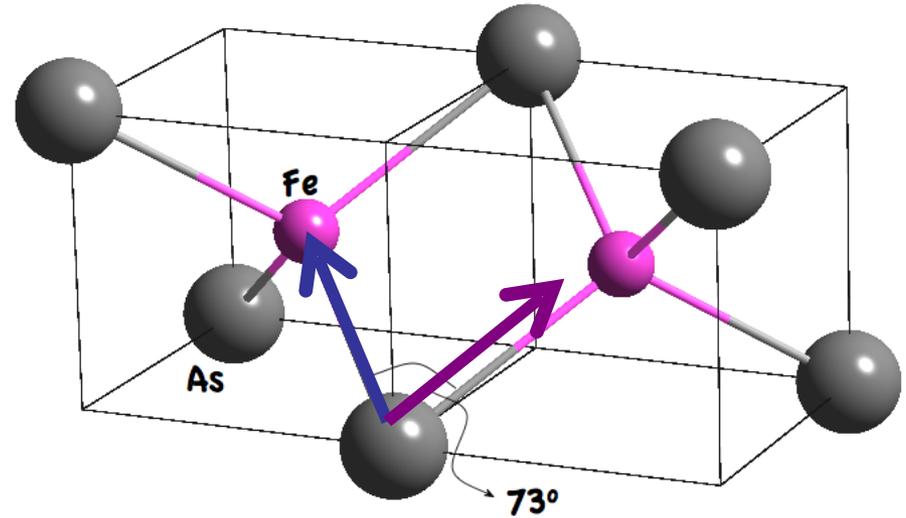
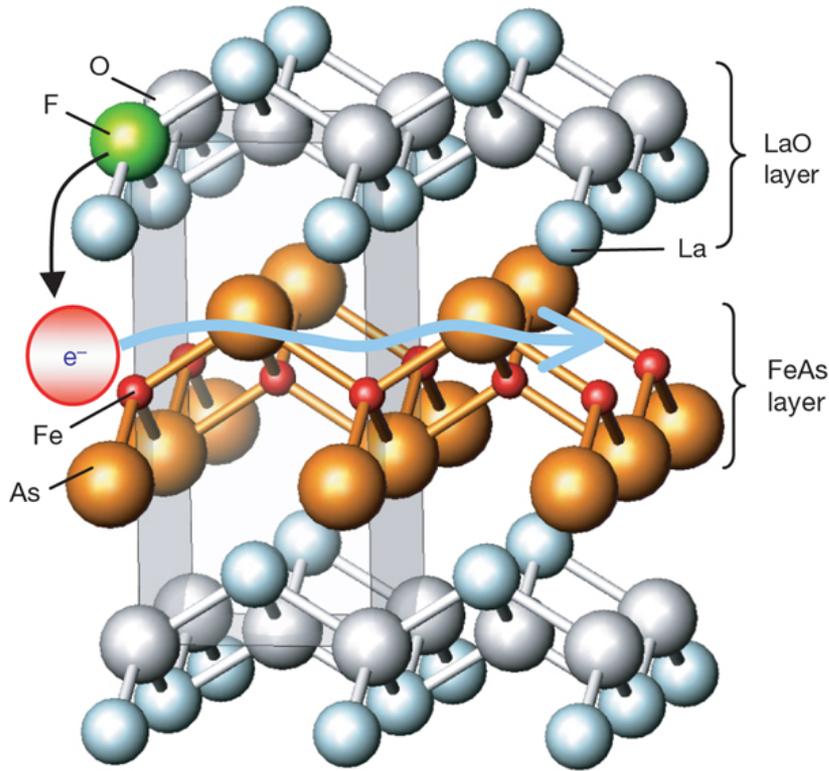
*two polarization fields
partially perpendicular*

*nearest neighbor V
is (partially) unscreened*



bond angle 90°

Screening of neighbor V on $BaFe_2As_2$ lattice

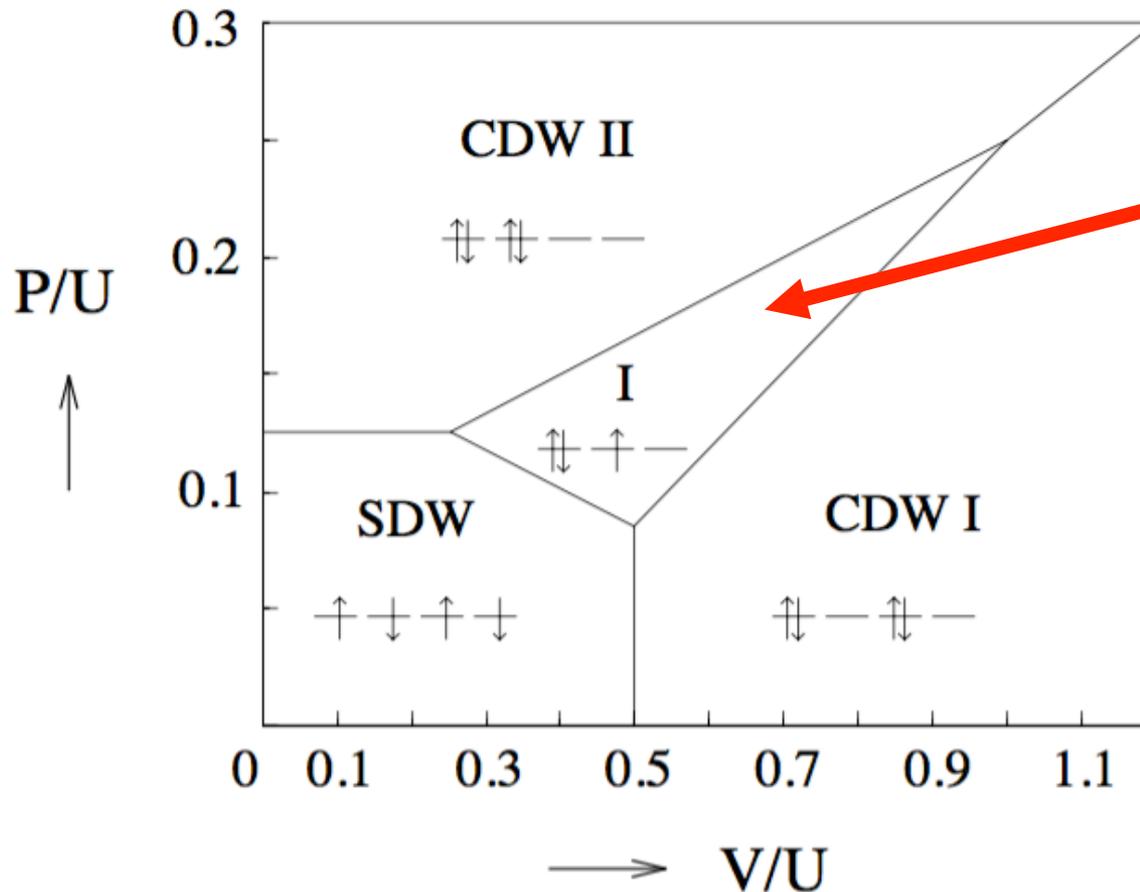


$$\alpha_{arsenic} \approx 10A^3$$

angle of 73° :
nearest neighbor V is overscreened

Sawatzky, Elfimov, JvdB, Zaanen
EPL 86, 17006 (2009)

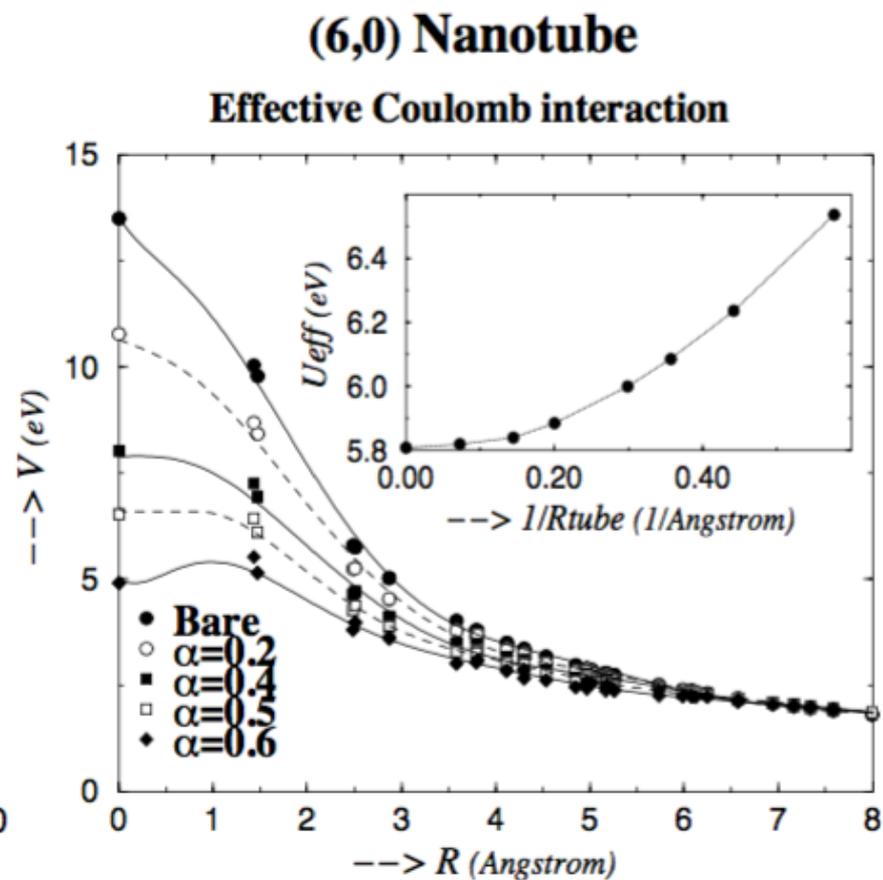
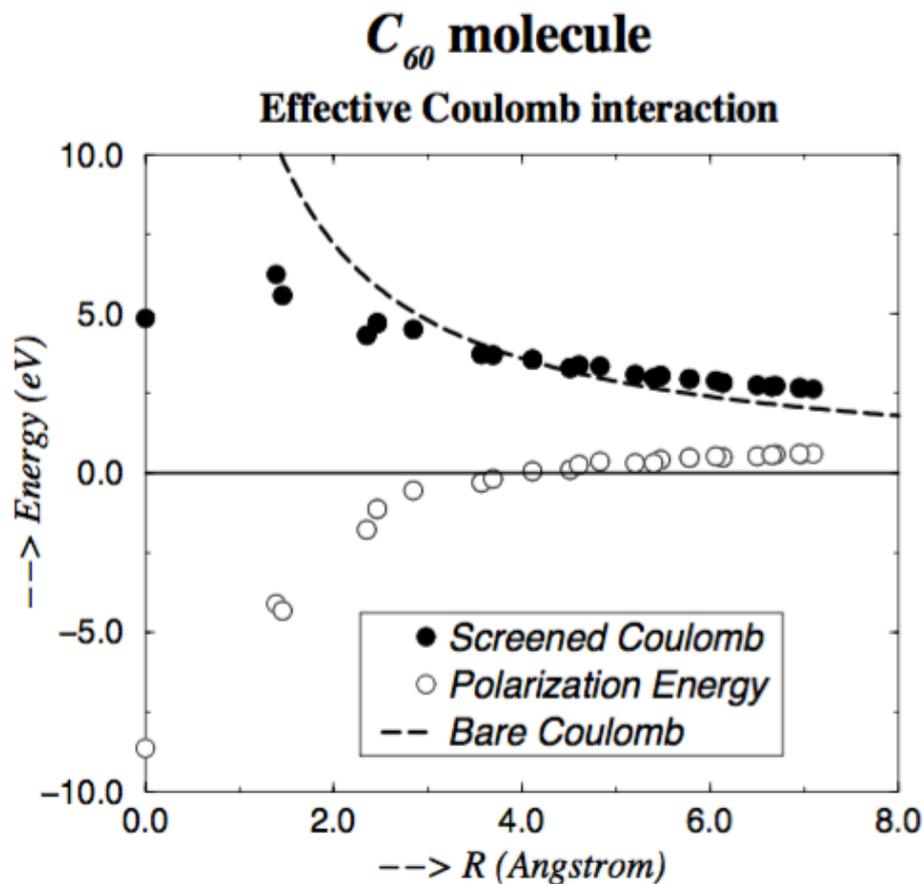
New types of charge order emerge



Broken inversion symmetry

JvdB, Meinders, Lorenzana, Eder & Sawatzky, PRL 75, 4658 (1995)

Screened interaction in nano systems

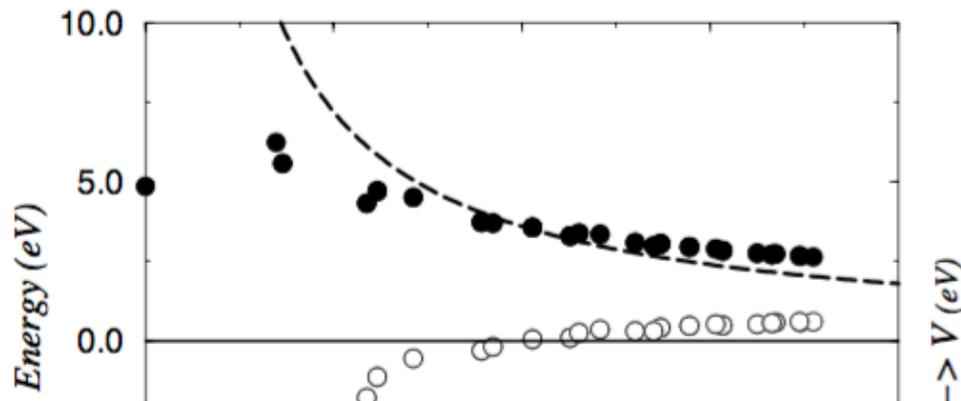


JvdB & Sawatzky, Electronic Properties of Novel Materials
- Progress in Molecular Nanostructures, 152 (1998)

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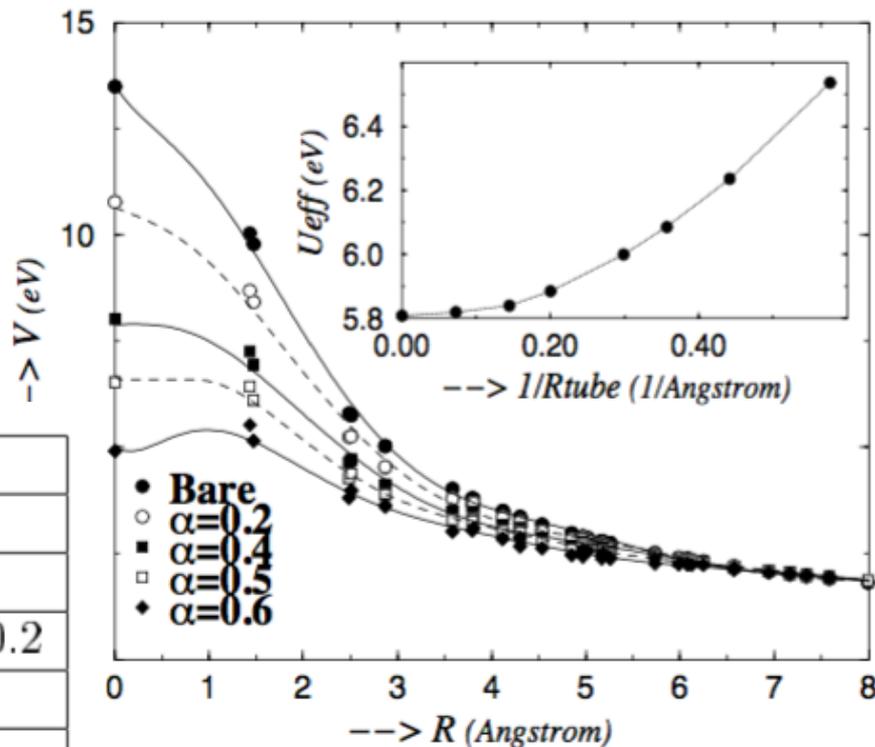
C_{60} molecule

Effective Coulomb interaction



(6,0) Nanotube

Effective Coulomb interaction

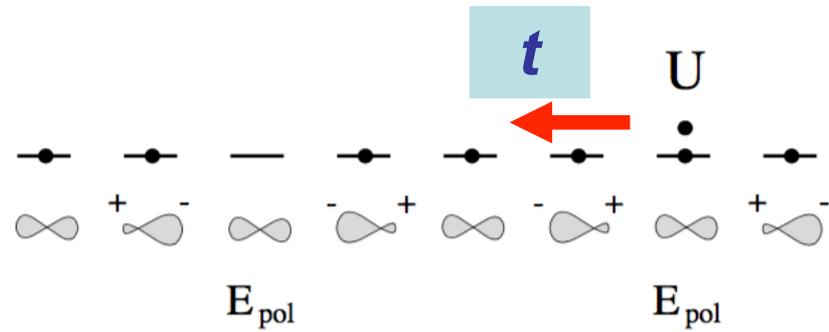


Effective Coulomb interaction for C_{60}

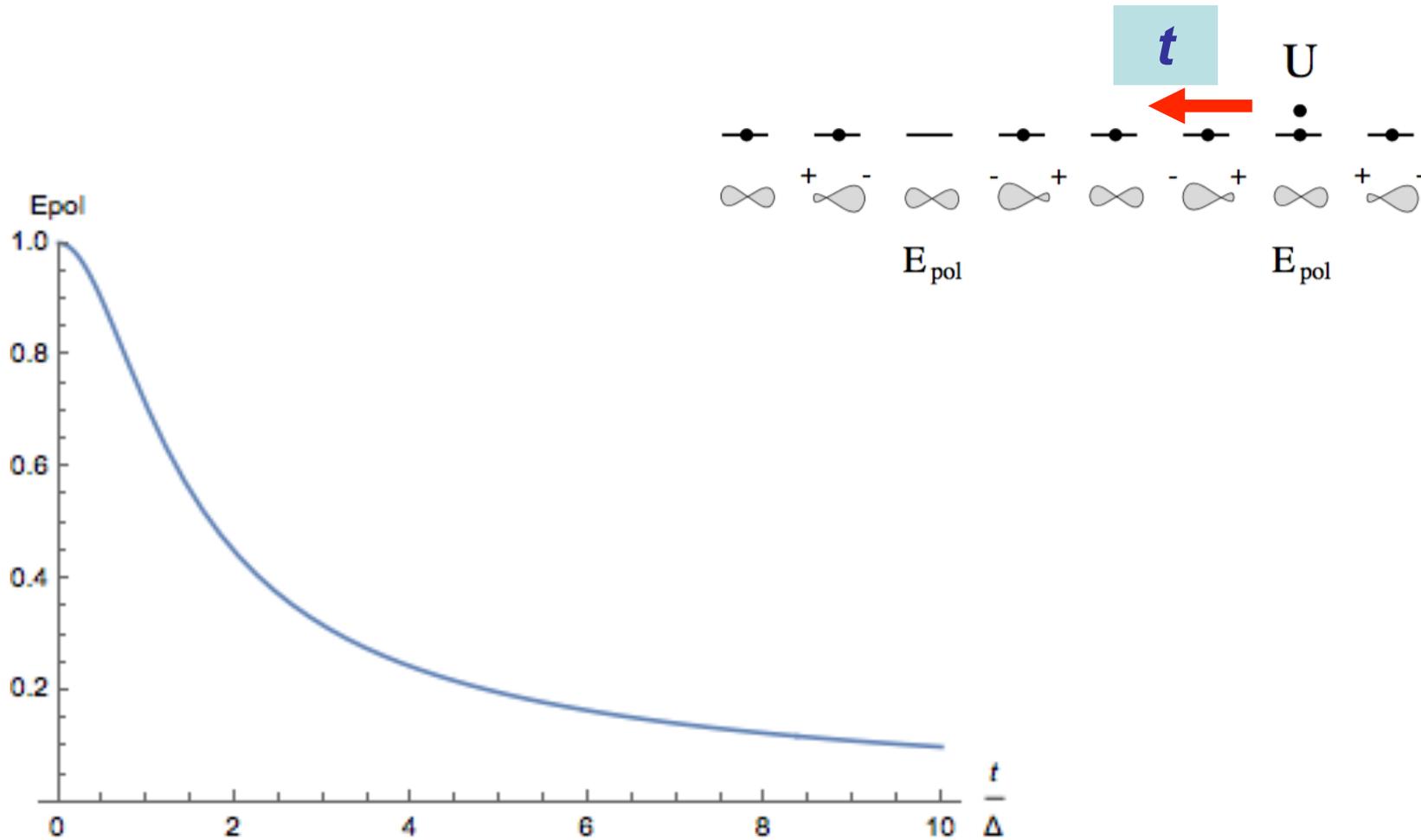
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Perturbative dependence of E_{pol} on t/Δ

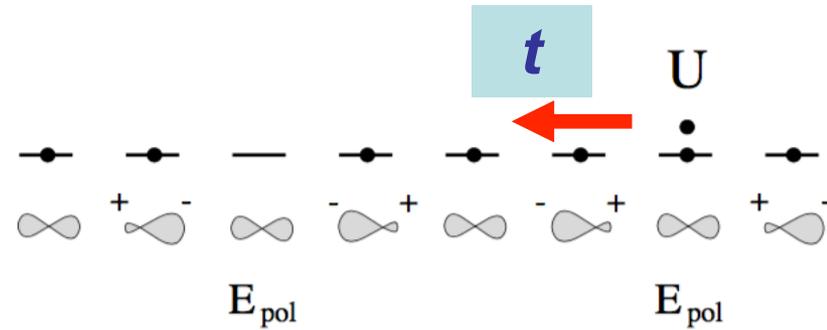
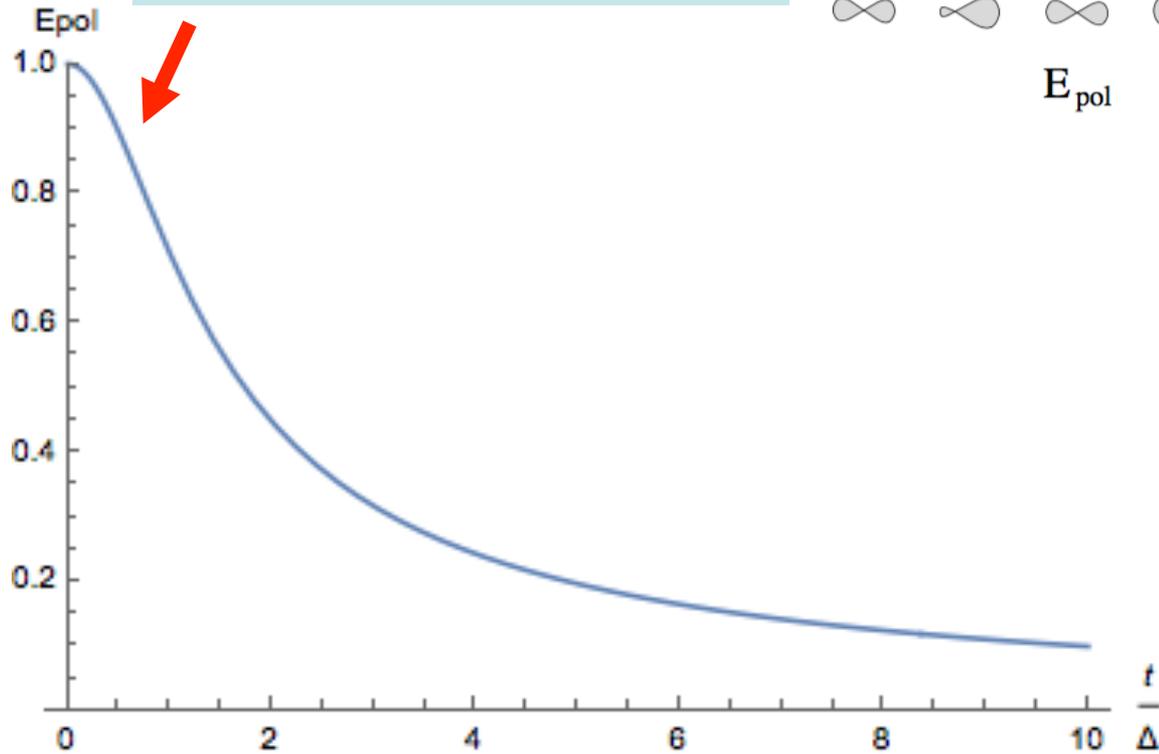


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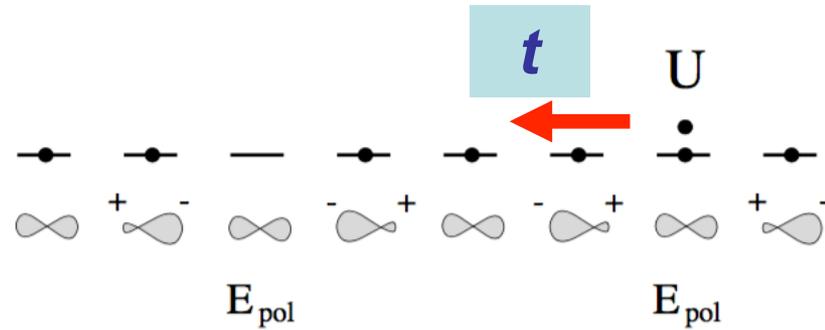
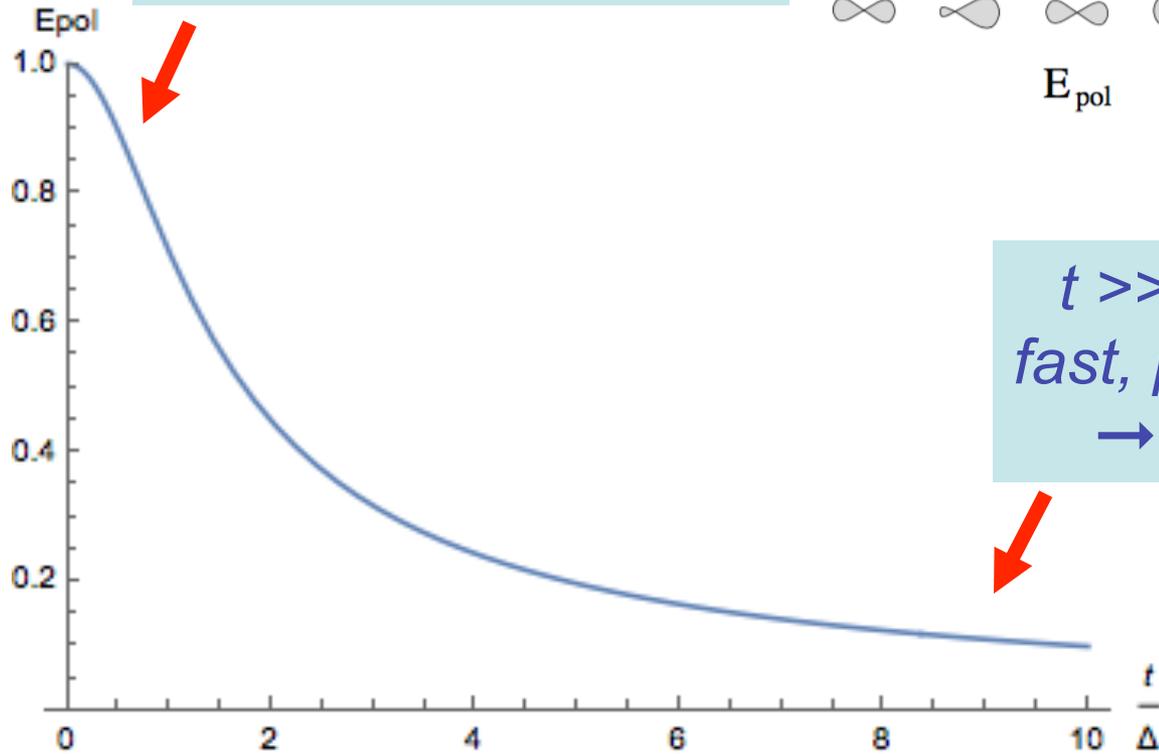
Perturbative dependence of E_{pol} on t/Δ

$t \ll \Delta \rightarrow$ electrons
slow, polarization fast
 \rightarrow static limit



Perturbative dependence of E_{pol} on t/Δ

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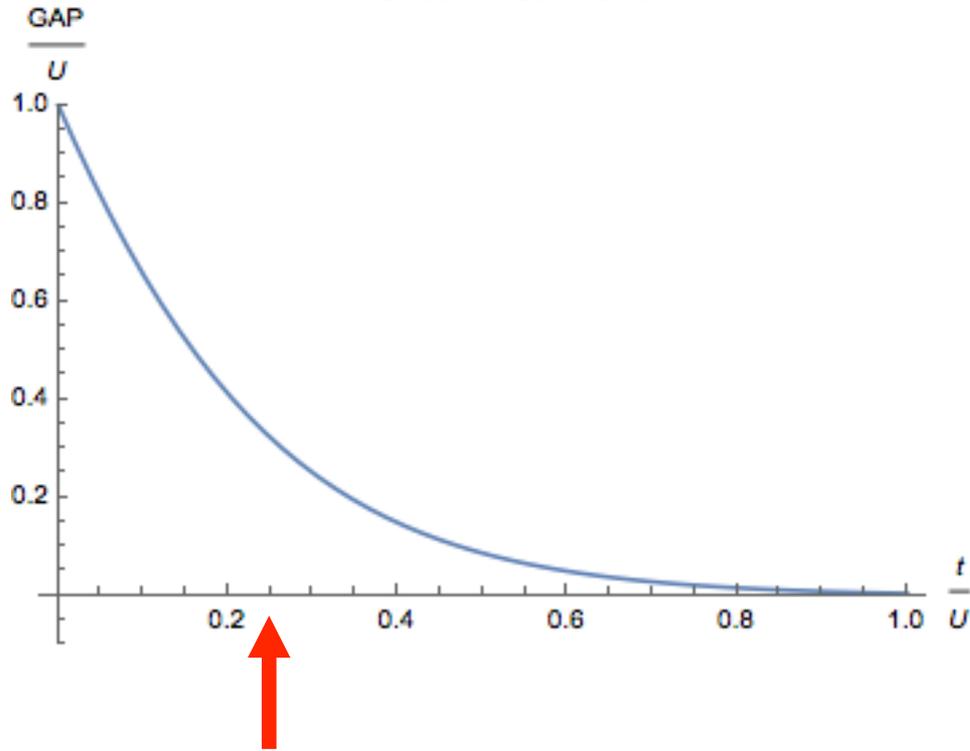


$t \gg \Delta \rightarrow$ electrons fast, polarization slow
 \rightarrow retarded limit

Apply to 1D Hubbard model

$$GAP = U - 4 - 8 \sum_{n=1}^{\infty} (-1)^n \left\{ \sqrt{1 + n^2 U^2 / 4} - nU/2 \right\}$$

1D Hubbard Lieb-Mattis

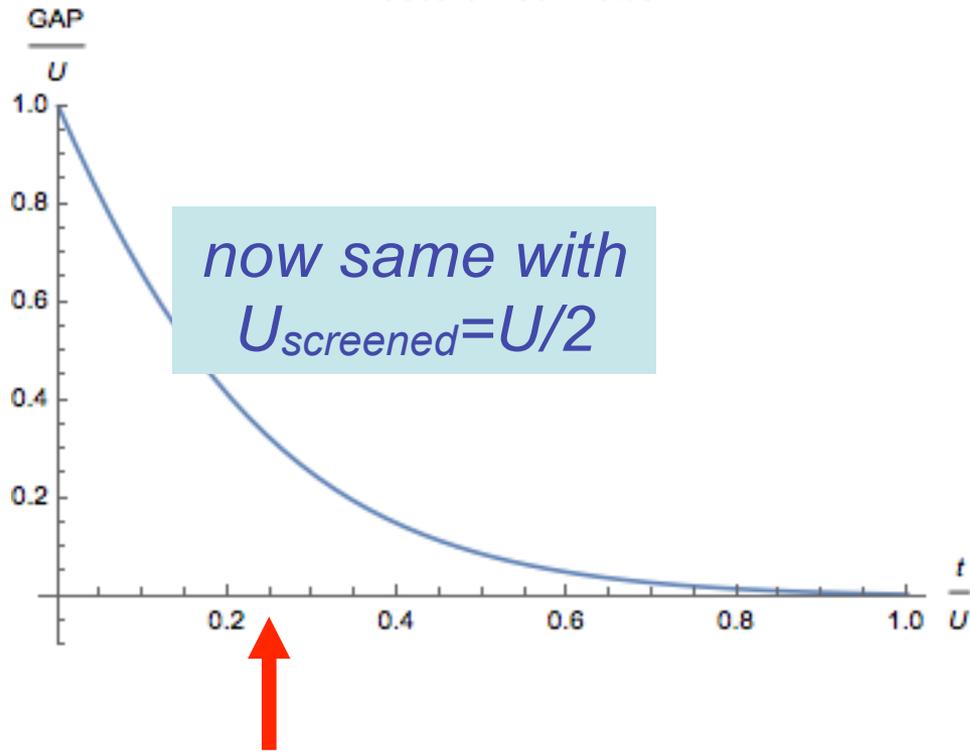


$U = 4t = \text{bandwidth}$

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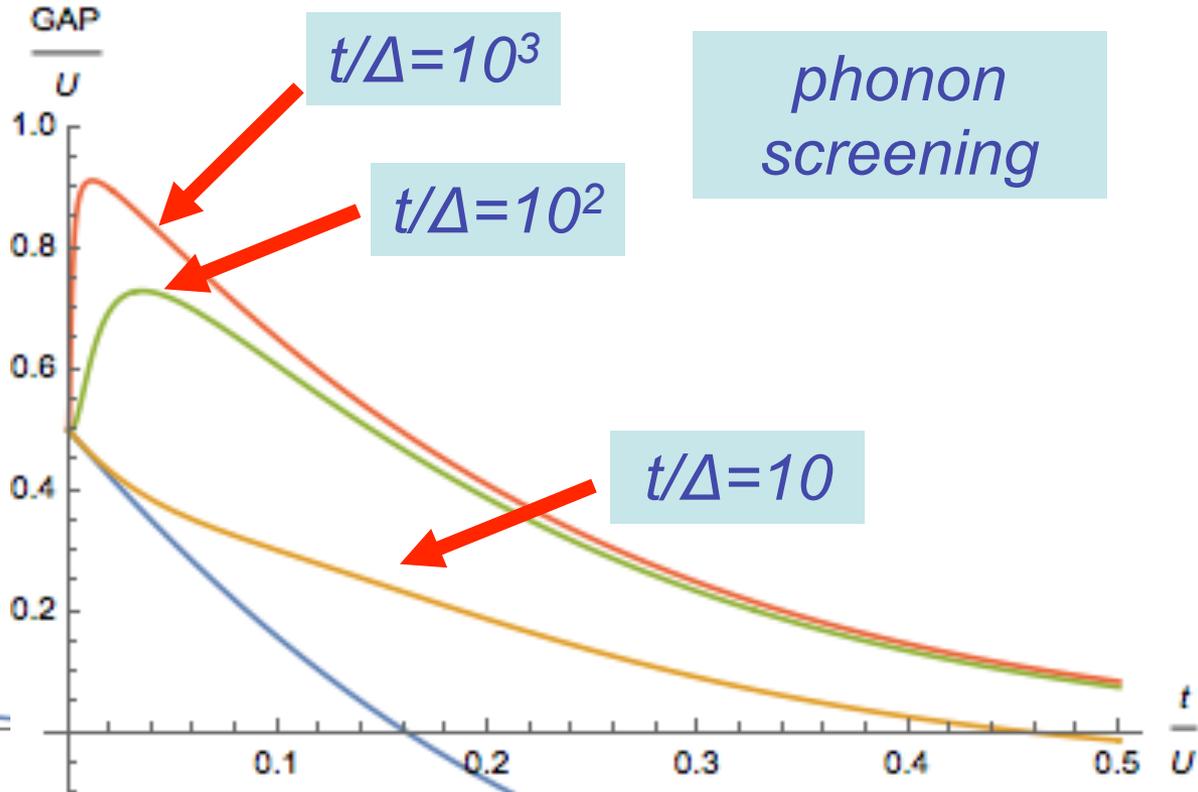
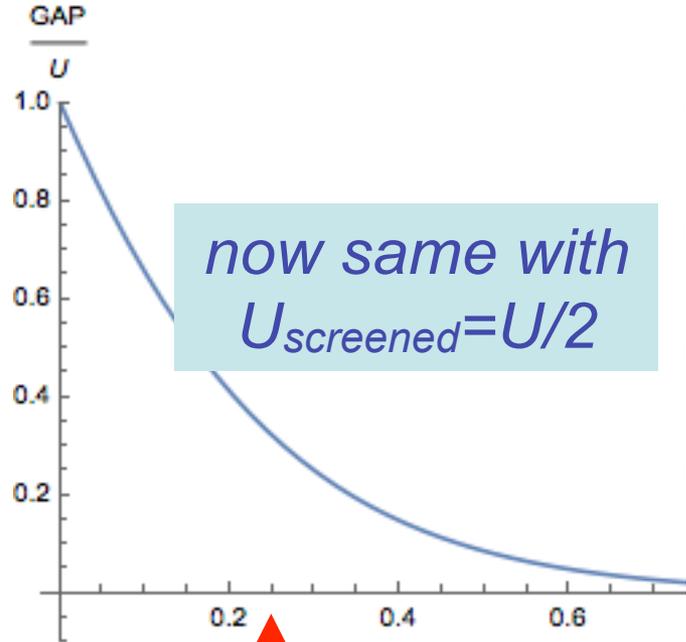


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1D Hubbard Lieb-Mattis



phonon screening

$t/\Delta = 1$

static limit

electronic screening

$U = 4t = \text{bandwidth}$

Relation to experiment: RIXS on Li_2CuO_2

ARTICLE

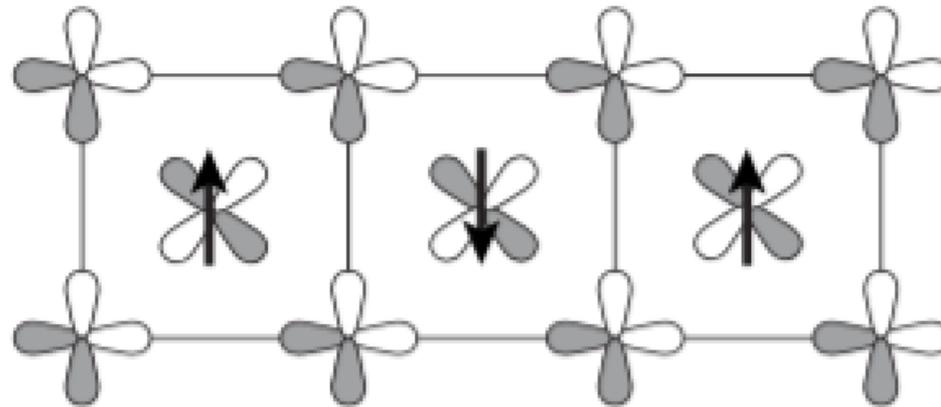
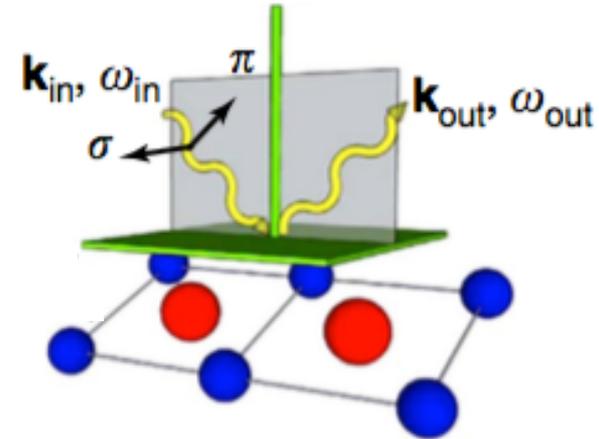
Received 10 Aug 2015 | Accepted 26 Dec 2015 | Published 17 Feb 2016

DOI: 10.1038/ncomms10563

OPEN

Electron-lattice interactions strongly renormalize the charge-transfer energy in the spin-chain cuprate Li_2CuO_2

Steve Johnston¹, Claude Monney^{2,3}, Valentina Bisogni^{4,5}, Ke-Jin Zhou^{2,6}, Roberto Kraus⁴, Günter Behr⁴, Vladimir N. Strocov², Jiří Málek⁷, Stefan-Ludwig Drechsler⁴, Jochen Geck⁴, Thorsten Schmitt² & Jeroen van den Brink^{4,8}



What is

Resonant

Inelastic

X-ray scattering

RIXS



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RIXS

X-ray scattering: photon in \rightarrow solid \rightarrow photon out

inelastic: $\omega_{out} < \omega_{in}$

resonant: tune ω_{in} to an atomic absorption edge

What is

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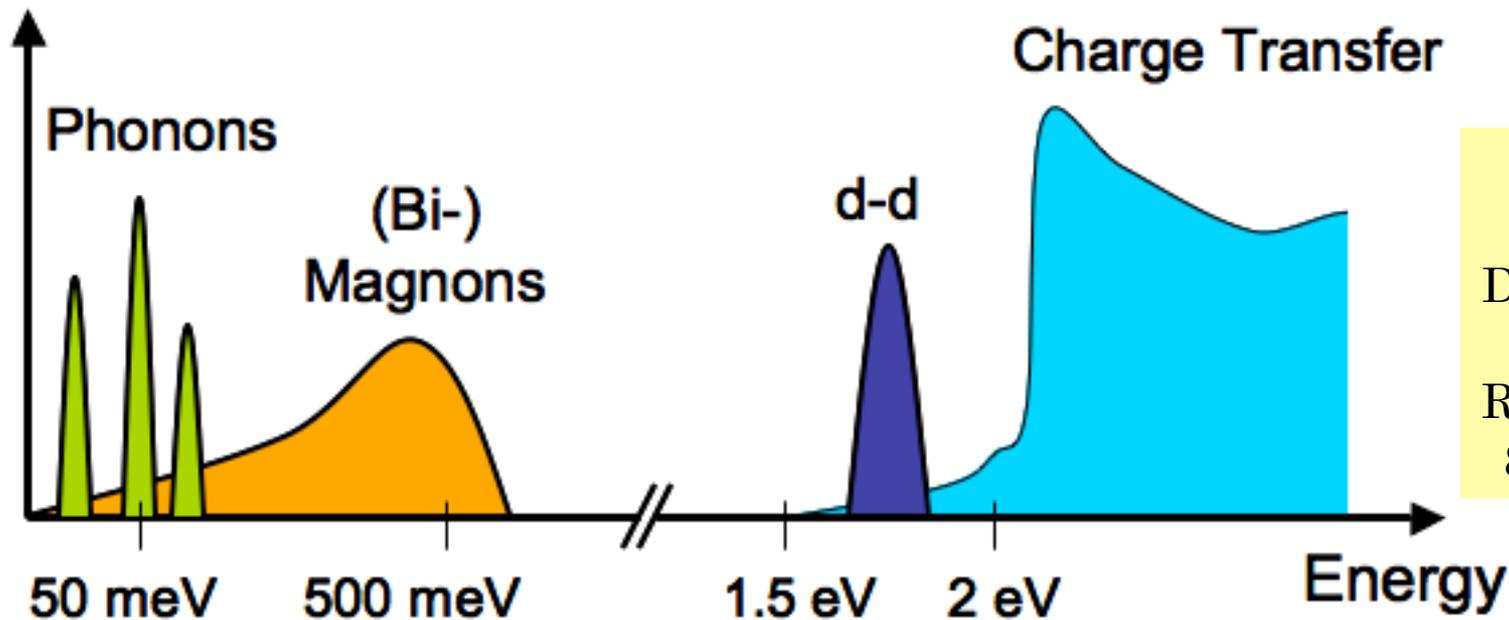
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Ament, van Veenendaal, Devereaux, Hill & JvdB
Rev. Mod. Phys. 83, 705 (2011)

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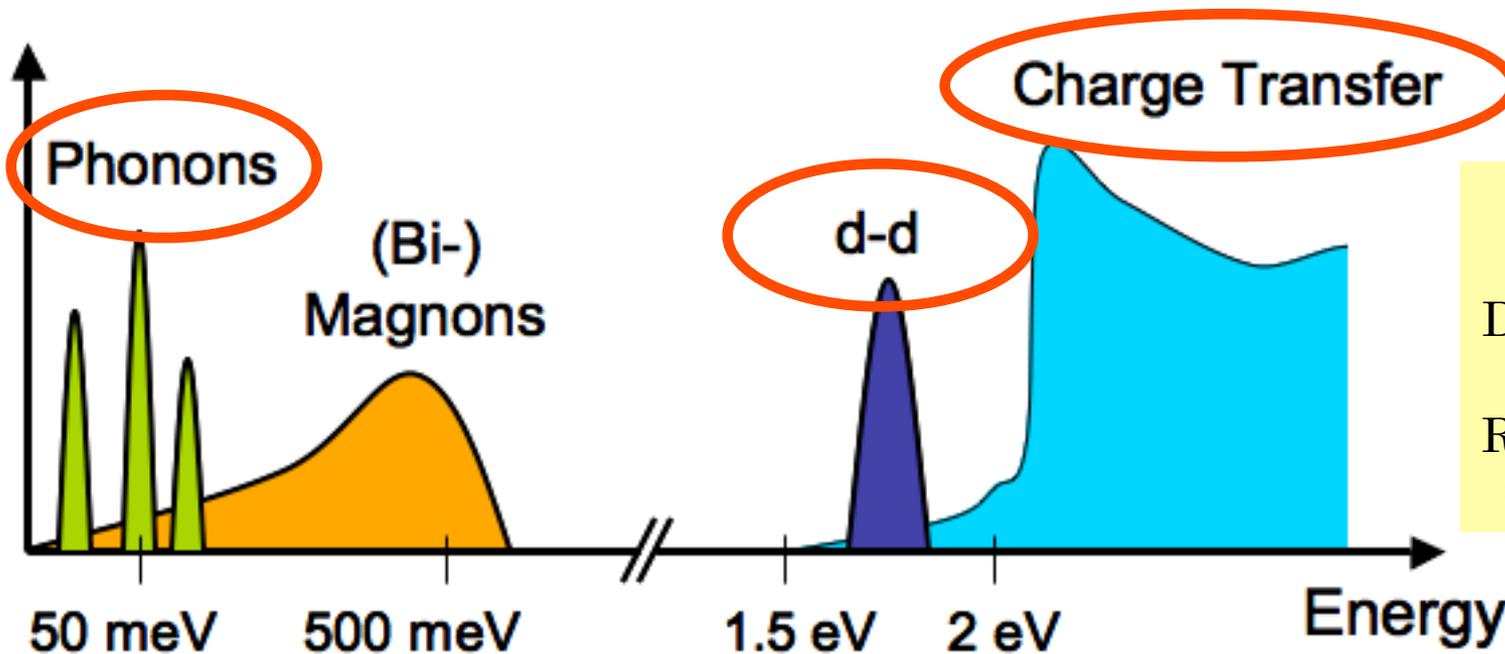
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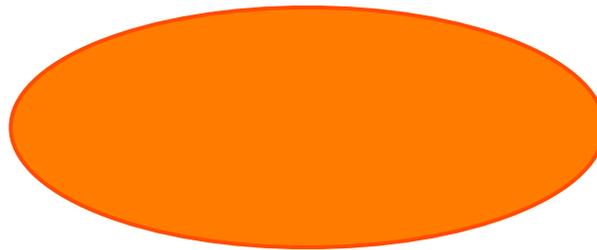
Cu

K-edge

4 p



~9 KeV



1 s



What is

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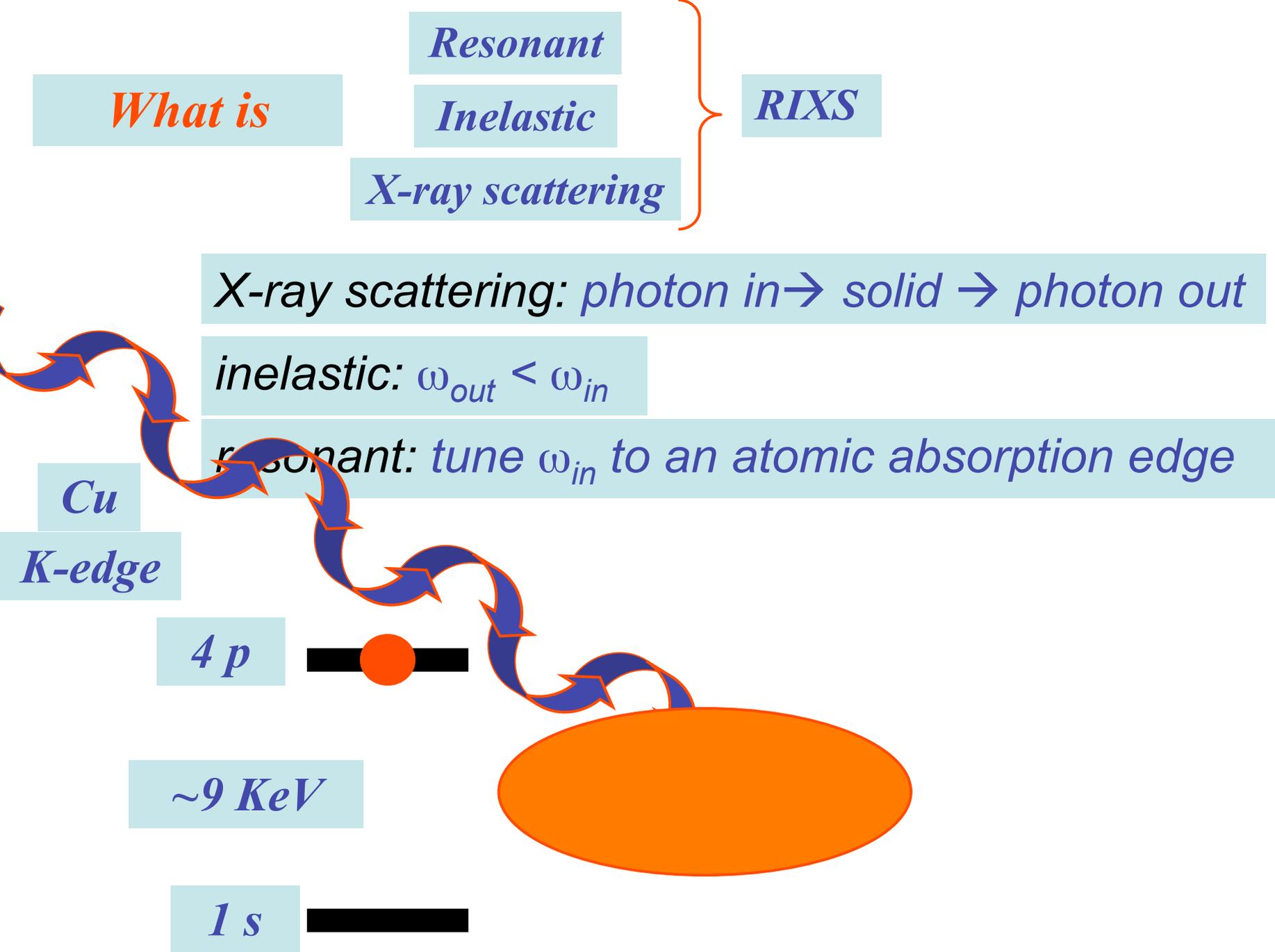
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Momentum transfer: q

Energy loss

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X-ray scattering

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X-ray scattering: photon in \rightarrow solid \rightarrow photon out

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INDIRECT

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1 s

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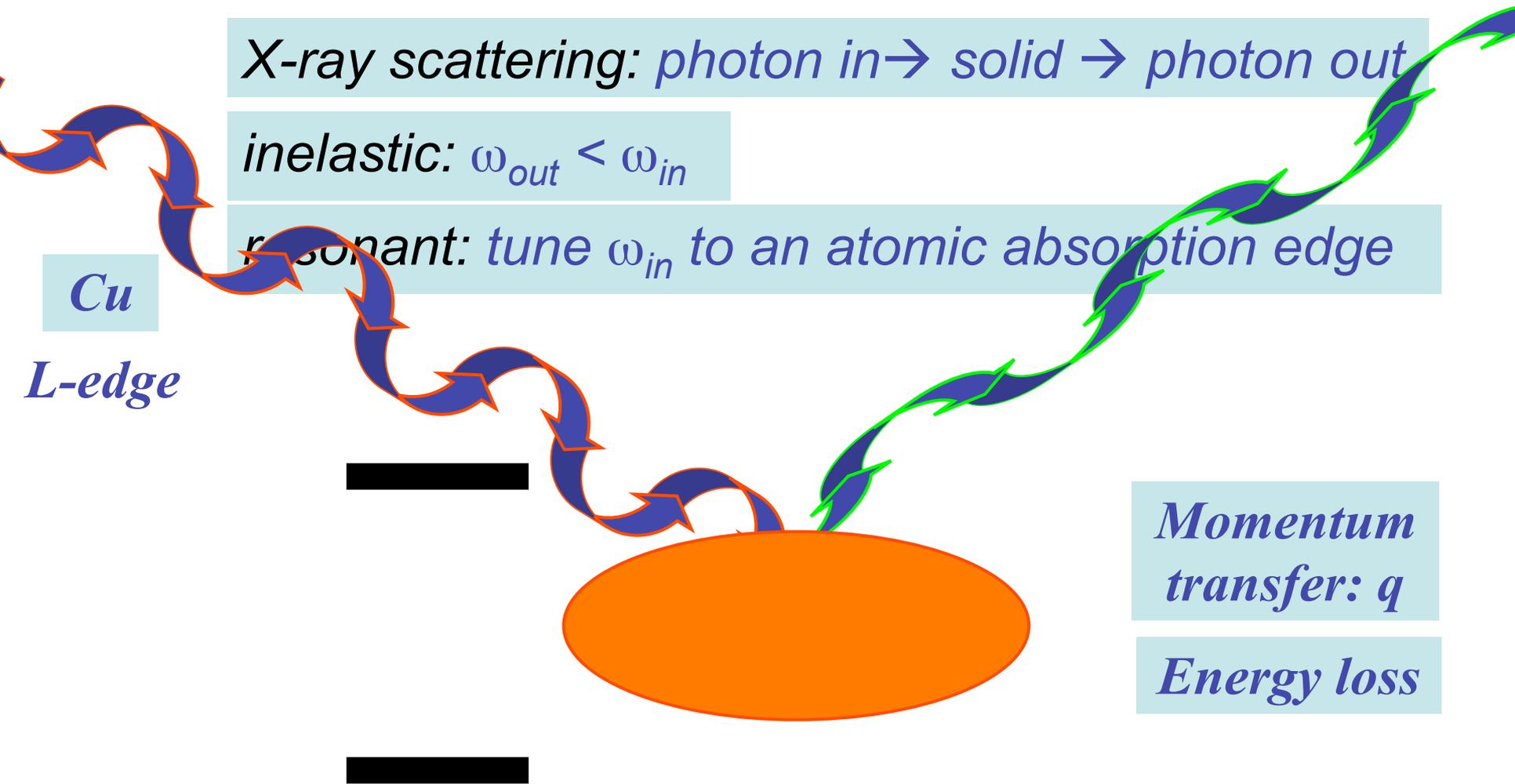
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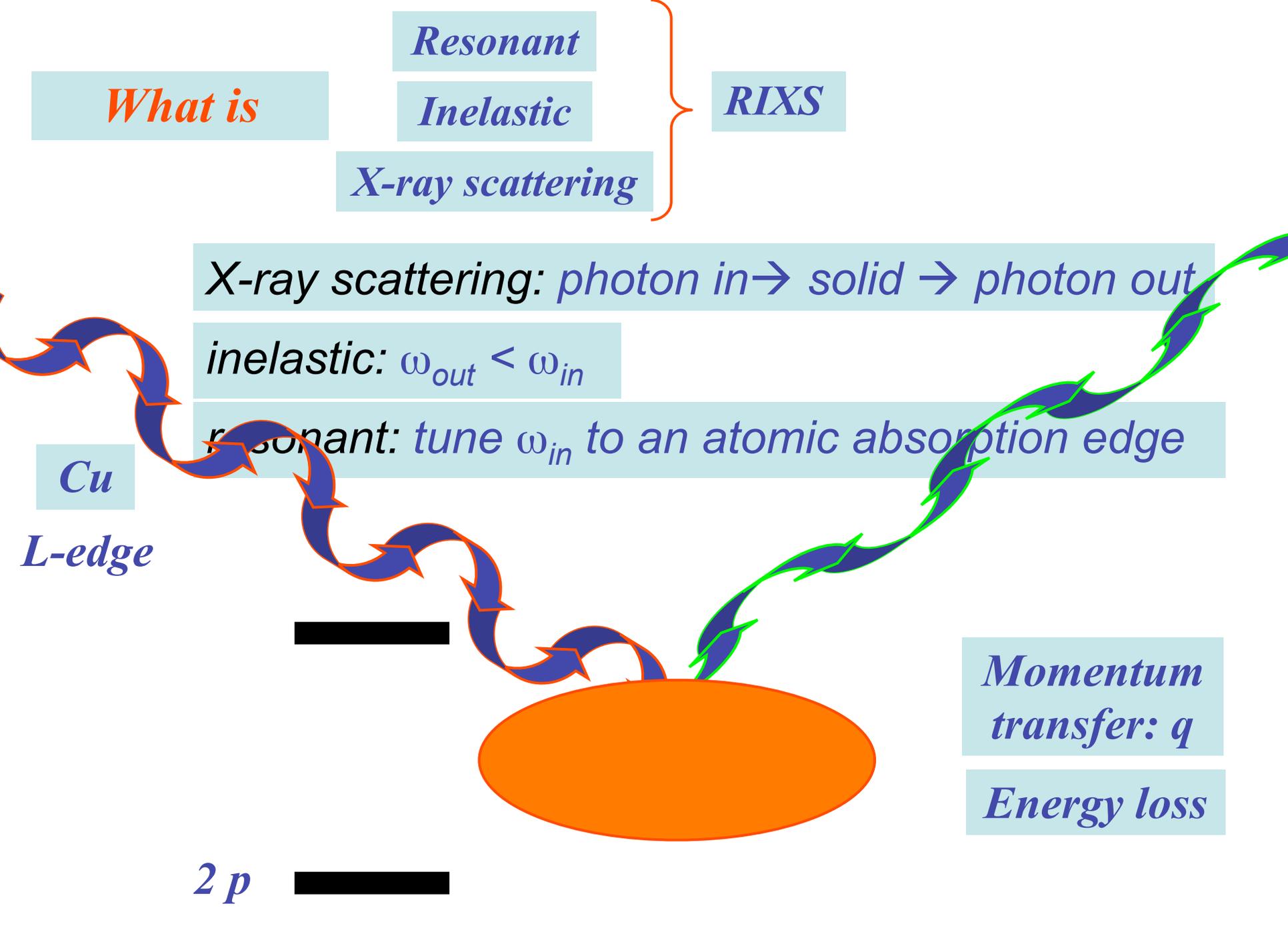
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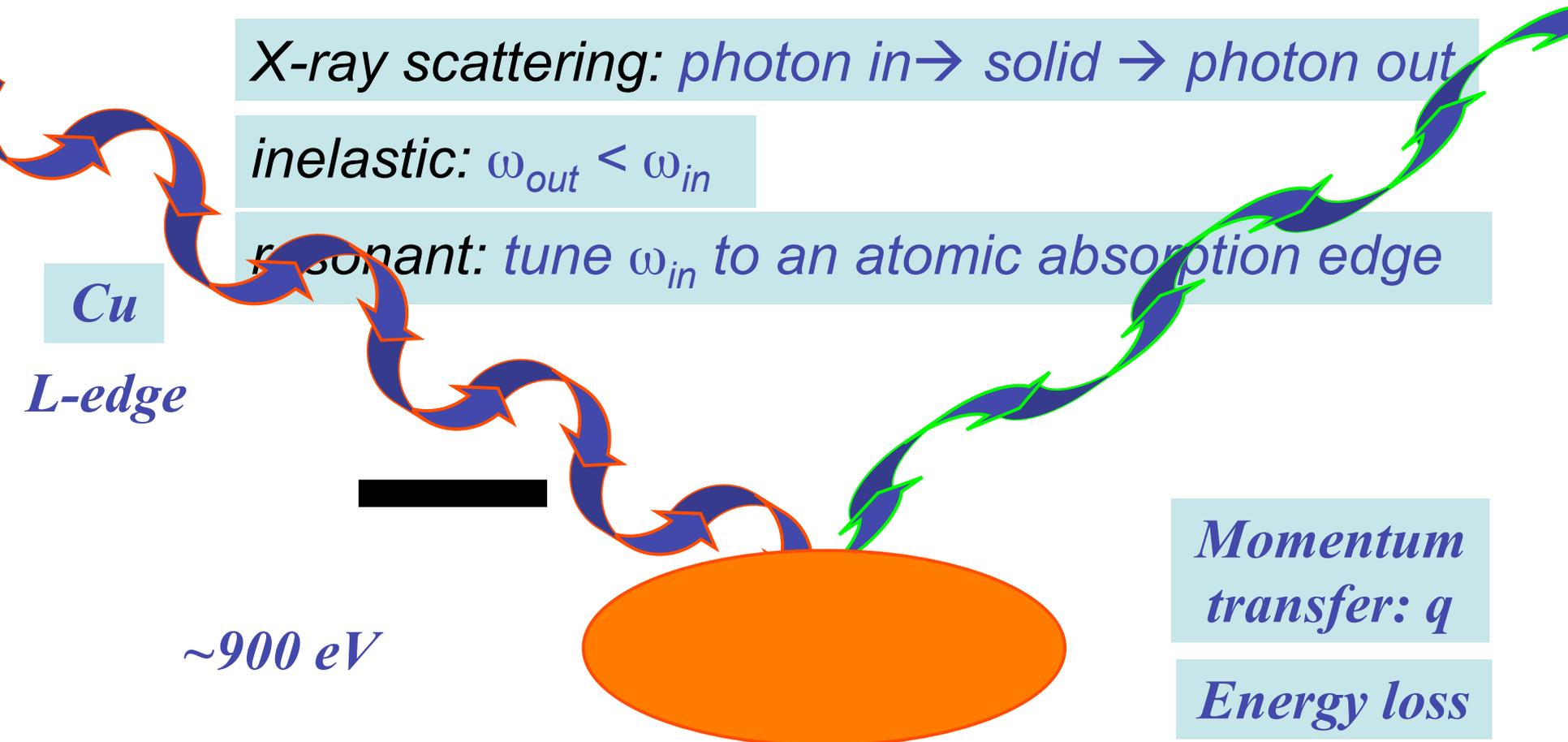
L-edge

~ 900 eV

$2p$

Momentum transfer: q

Energy loss



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X-ray scattering

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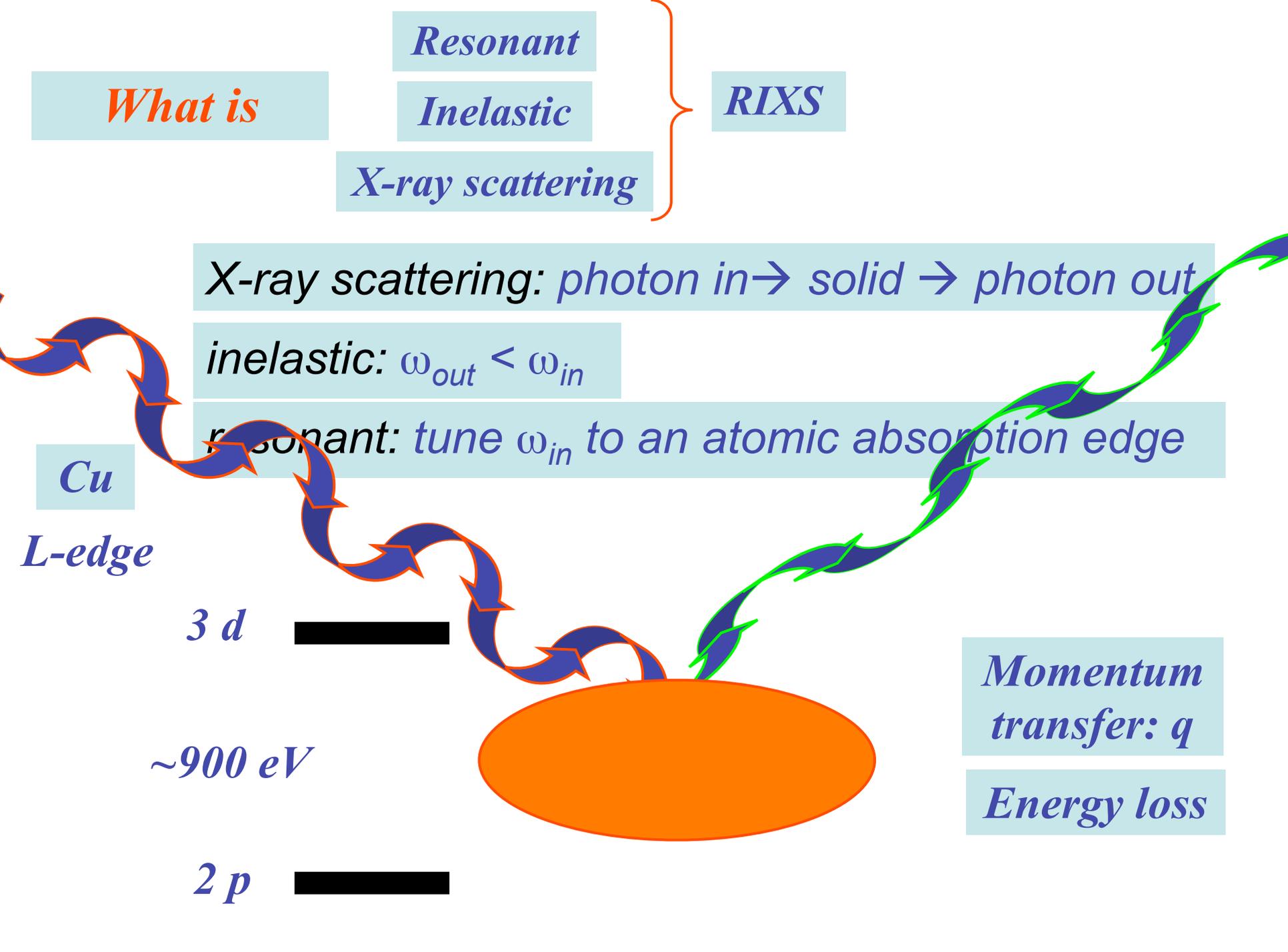
3 d

~ 900 eV

2 p

Momentum transfer: q

Energy loss



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X-ray scattering

RIXS

X-ray scattering: photon in \rightarrow solid \rightarrow photon out

inelastic: $\omega_{out} < \omega_{in}$

resonant: tune ω_{in} to an atomic absorption edge

Cu

L-edge

DIRECT

3 d

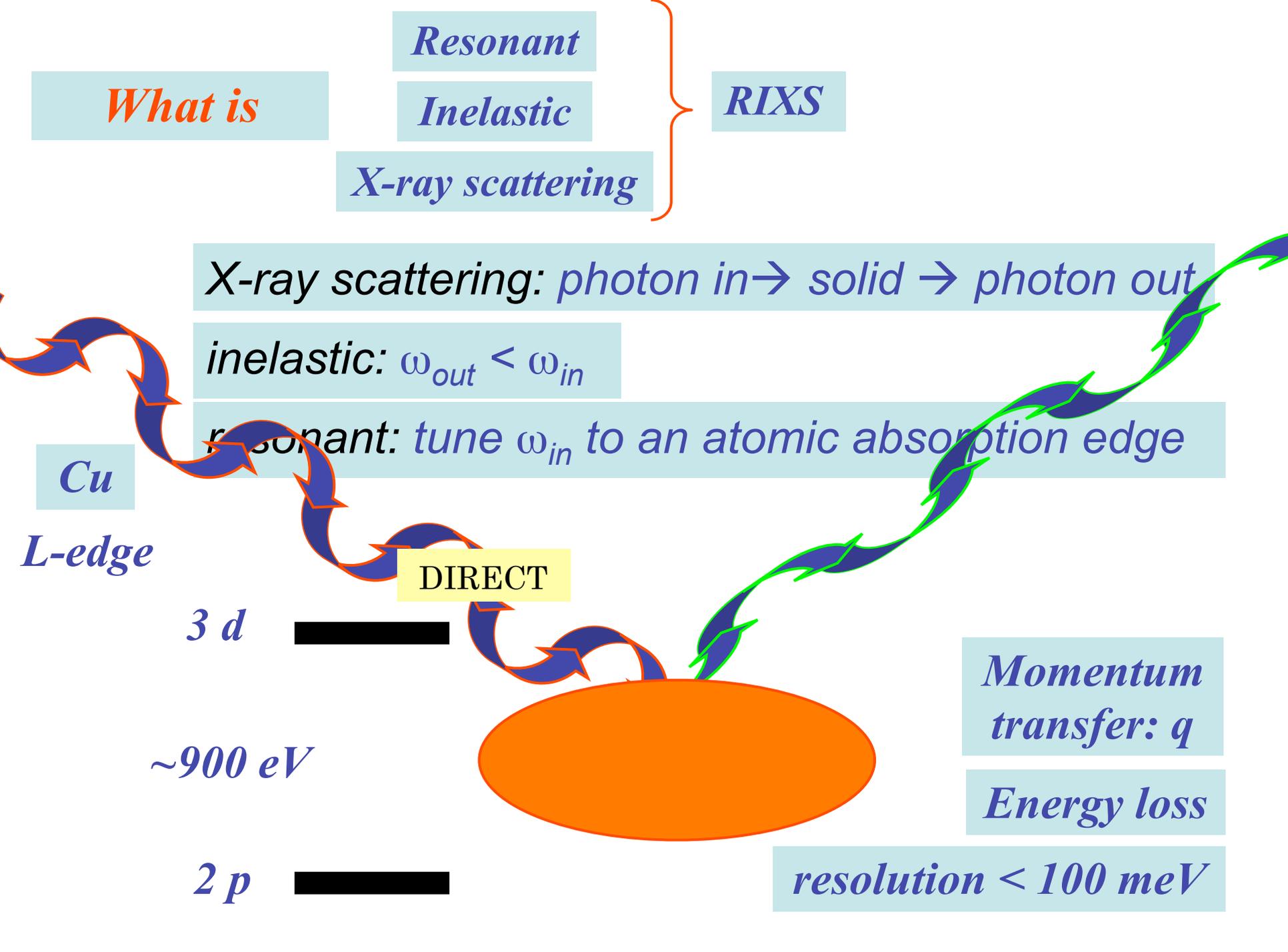
~ 900 eV

2 p

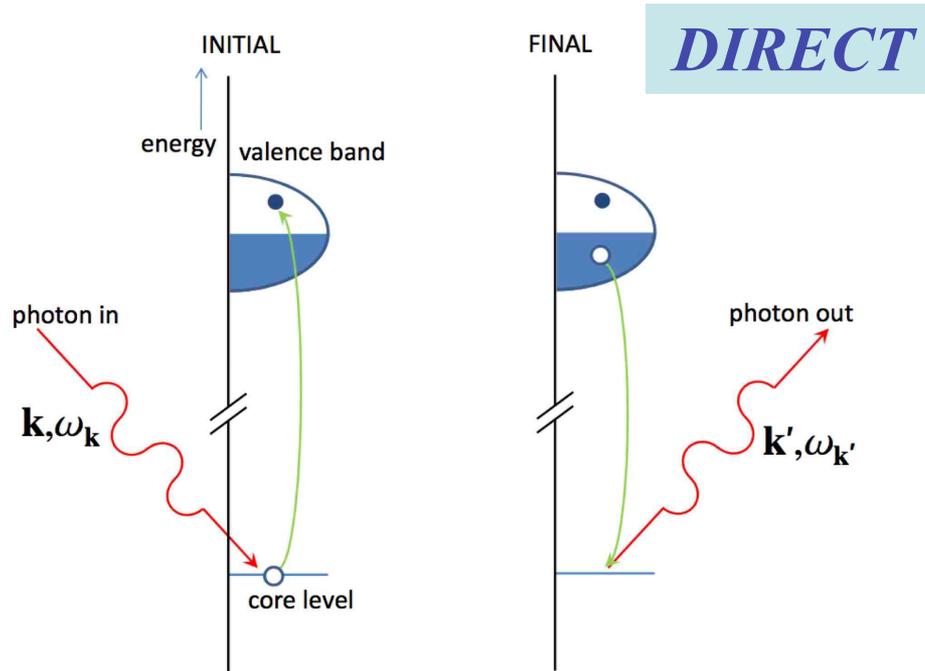
Momentum transfer: q

Energy loss

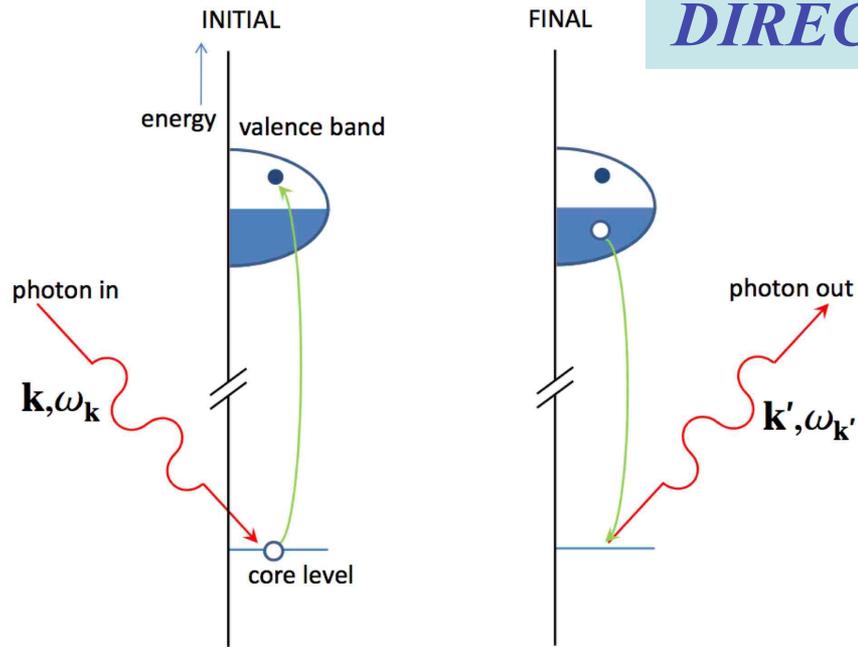
resolution < 100 meV



Direct and Indirect RIXS



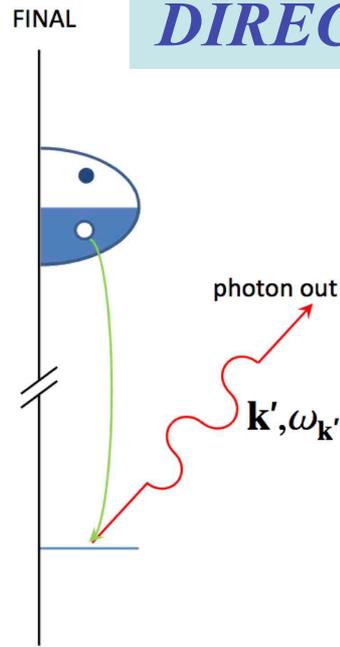
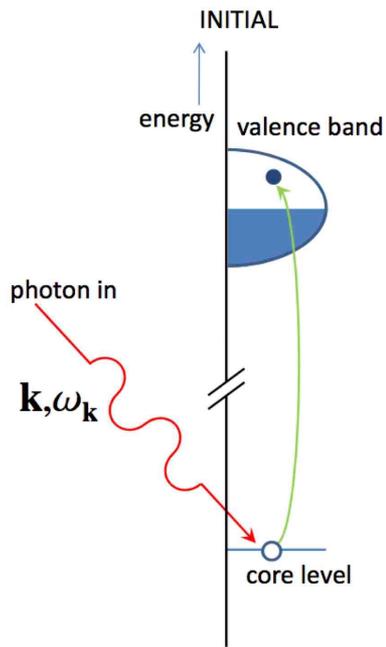
Direct and Indirect RIXS



DIRECT

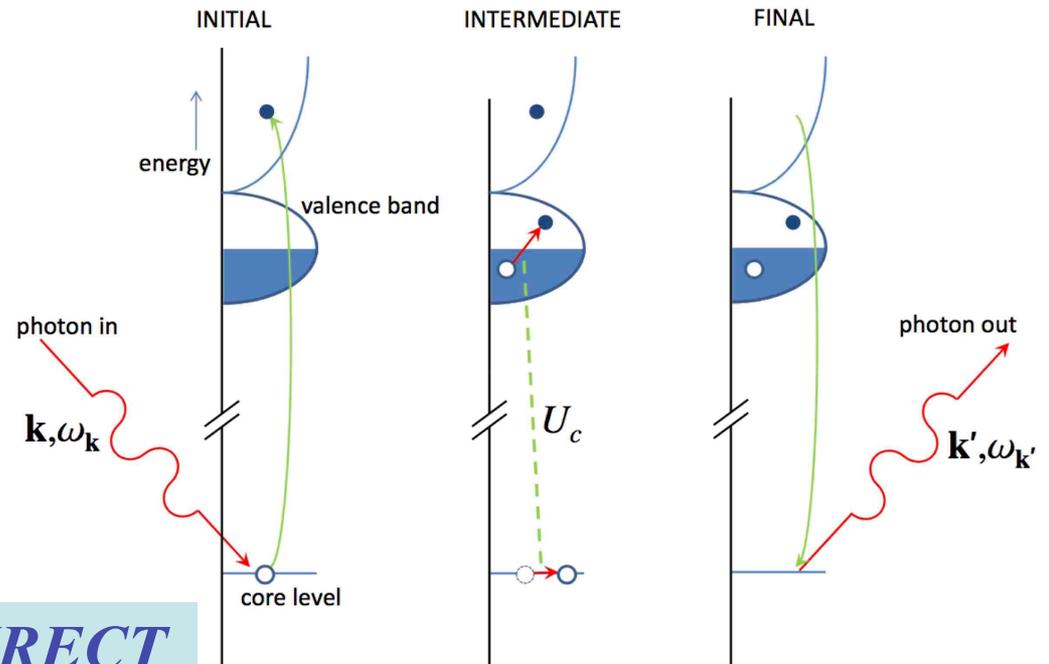
scattering via absorption-emission matrix elements

Direct and Indirect RIXS



DIRECT

scattering via absorption-emission matrix elements

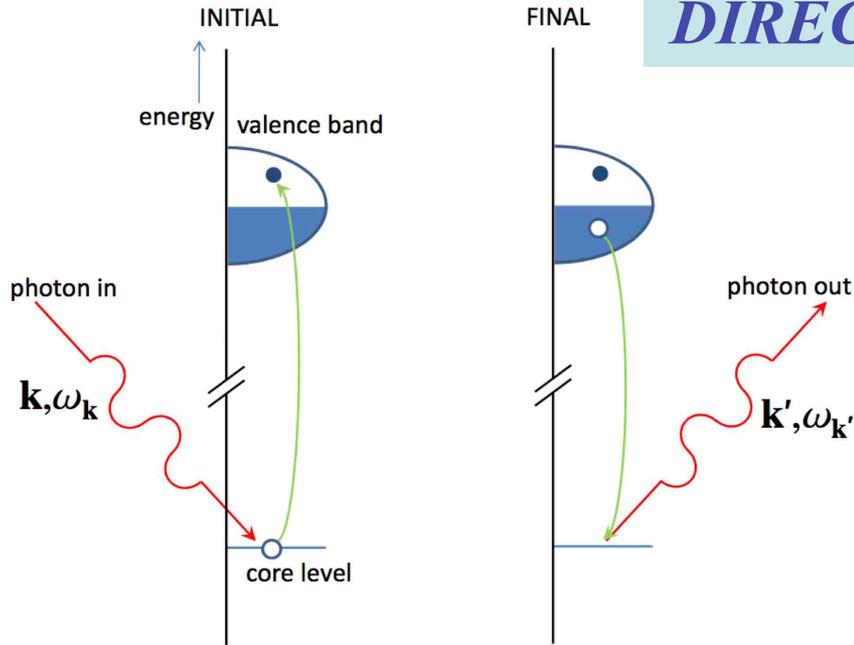


INDIRECT

Direct and Indirect RIXS

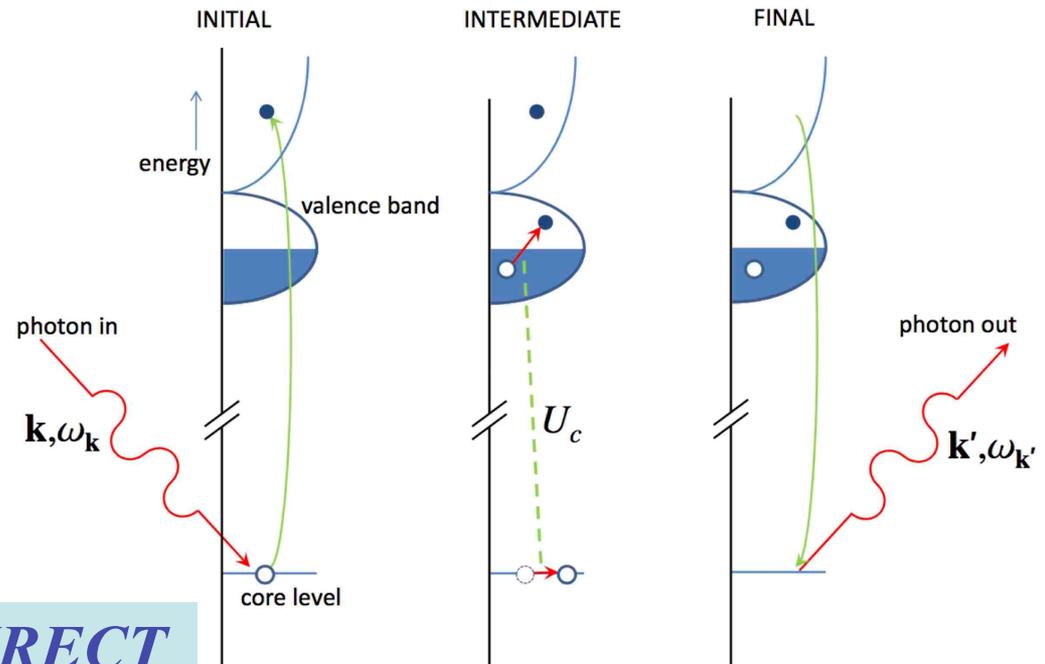
DIRECT

scattering via absorption-emission matrix elements



scattering via intermediate state core-hole shake-up

INDIRECT



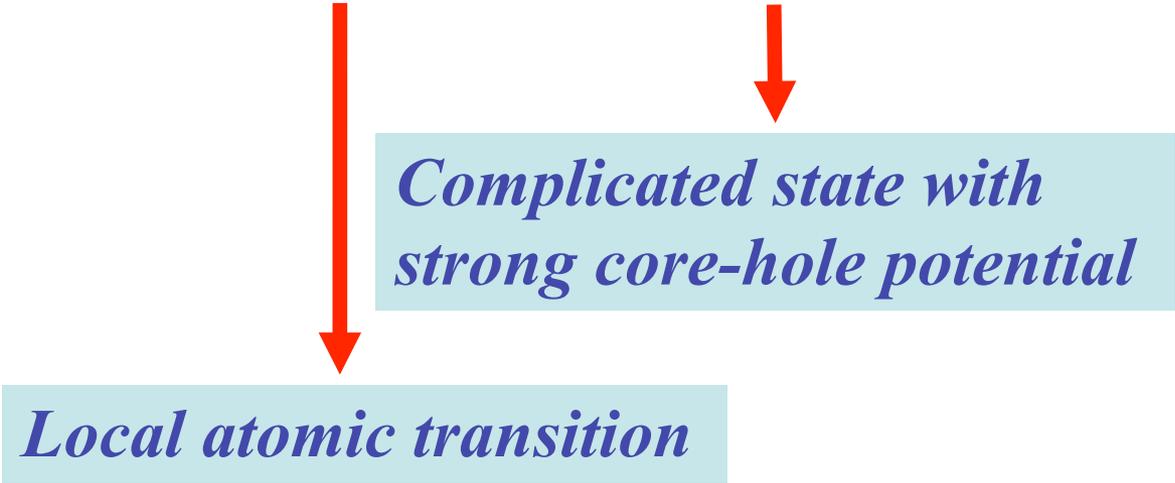
RIXS = $|GS\rangle \rightarrow XAS \rightarrow |INTERMEDIATE\rangle \rightarrow XES \rightarrow |FS\rangle$

RIXS = |GS⟩ → XAS → |INTERMEDIATE⟩ → XES → |FS⟩



Local atomic transition

RIXS = |GS⟩ → XAS → |INTERMEDIATE⟩ → XES → |FS⟩



*Complicated state with
strong core-hole potential*

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Local atomic transition

Local atomic transition

Contains chemical detail and atom specific physics

But:

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RIXS can probe universal effective low energy behavior

Resonant Scattering Intensity

*RIXS
amplitude*

$$\mathcal{F}_{fg}(\mathbf{k}, \mathbf{k}', \epsilon, \epsilon', \omega_{\mathbf{k}}, \omega_{\mathbf{k}'}) = \sum_n \frac{\langle f | \mathcal{D}'^\dagger | n \rangle \langle n | \mathcal{D} | g \rangle}{E_g + \hbar\omega_{\mathbf{k}} - E_n + i\Gamma_n}$$

Kramers-Heisenberg expression

Resonant Scattering Intensity

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Kramers-Heisenberg expression

*RIXS
transition
operator*

$$\mathcal{D} = \frac{1}{im\omega_{\mathbf{k}}} \sum_{i=1}^N e^{i\mathbf{k} \cdot \mathbf{r}_i} \boldsymbol{\epsilon} \cdot \mathbf{p}_i,$$

Resonant Scattering Intensity

RIXS
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Kramers-Heisenberg expression

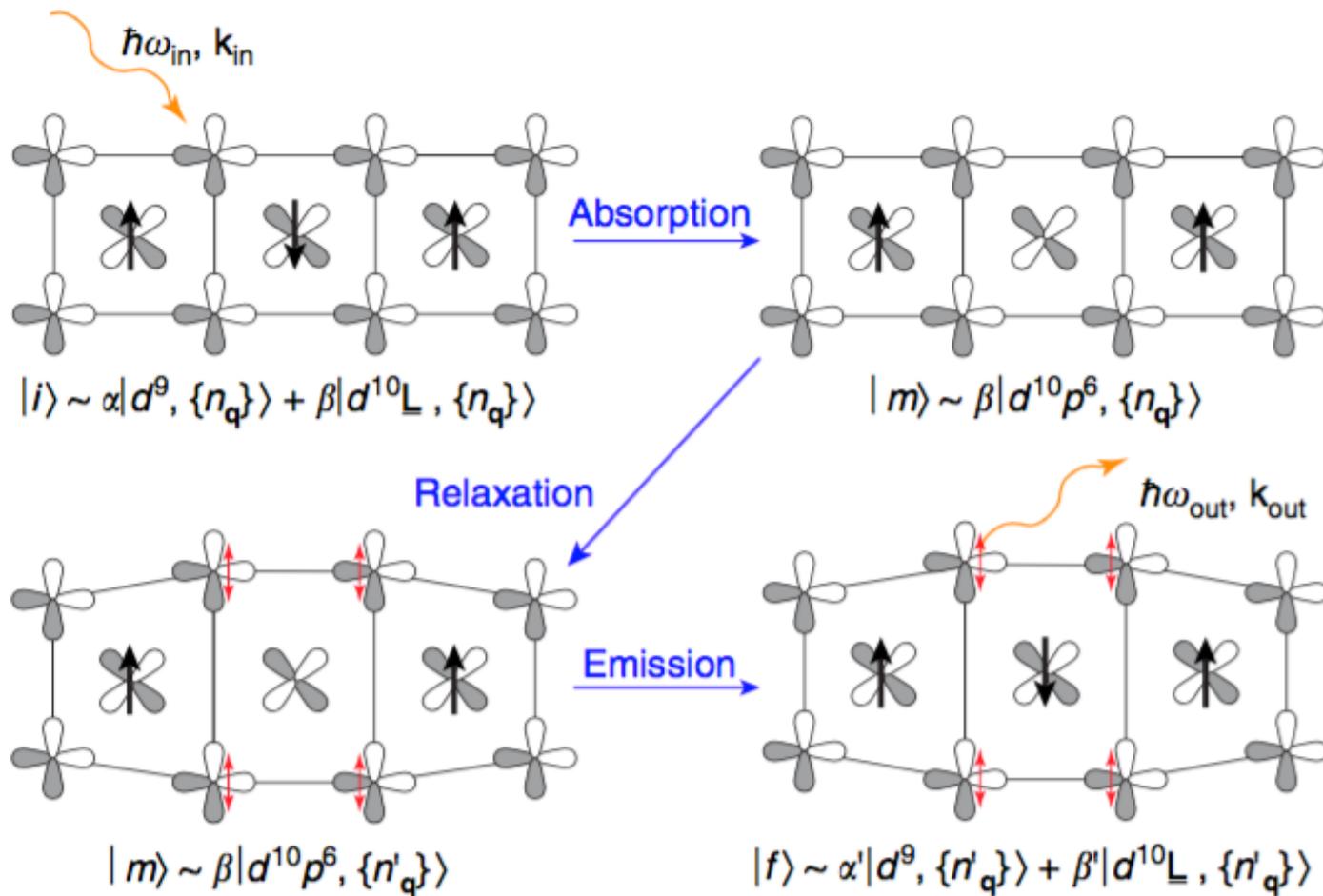
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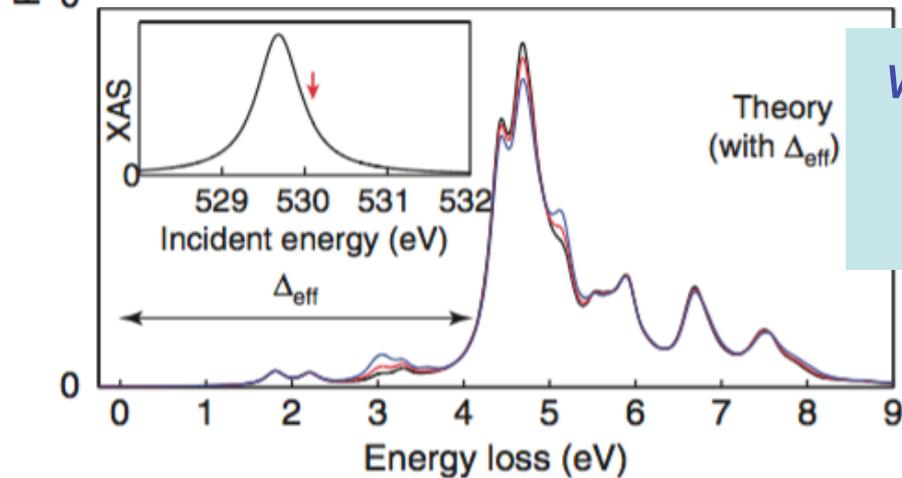
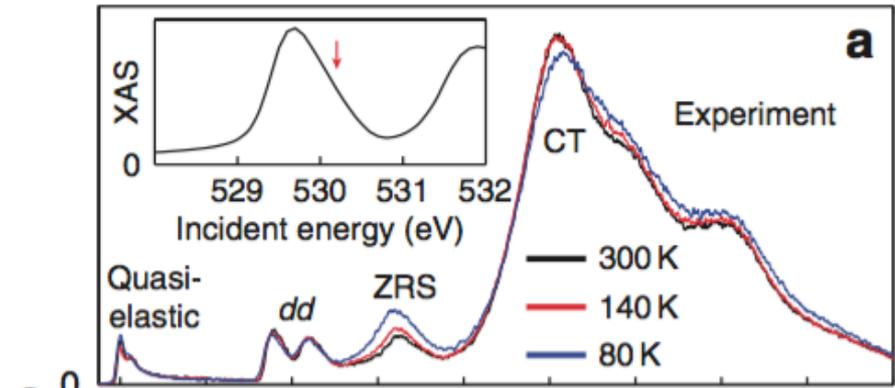
RIXS
intensity

$$I(\omega, \mathbf{k}, \mathbf{k}', \boldsymbol{\epsilon}, \boldsymbol{\epsilon}') = \sum_f |\mathcal{F}_{fg}(\mathbf{k}, \mathbf{k}', \boldsymbol{\epsilon}, \boldsymbol{\epsilon}', \omega_{\mathbf{k}})|^2 \\ \times \delta(E_f + \hbar\omega_{\mathbf{k}'} - E_g - \hbar\omega_{\mathbf{k}})$$

Oxygen K-edge RIXS on Li_2CuO_2

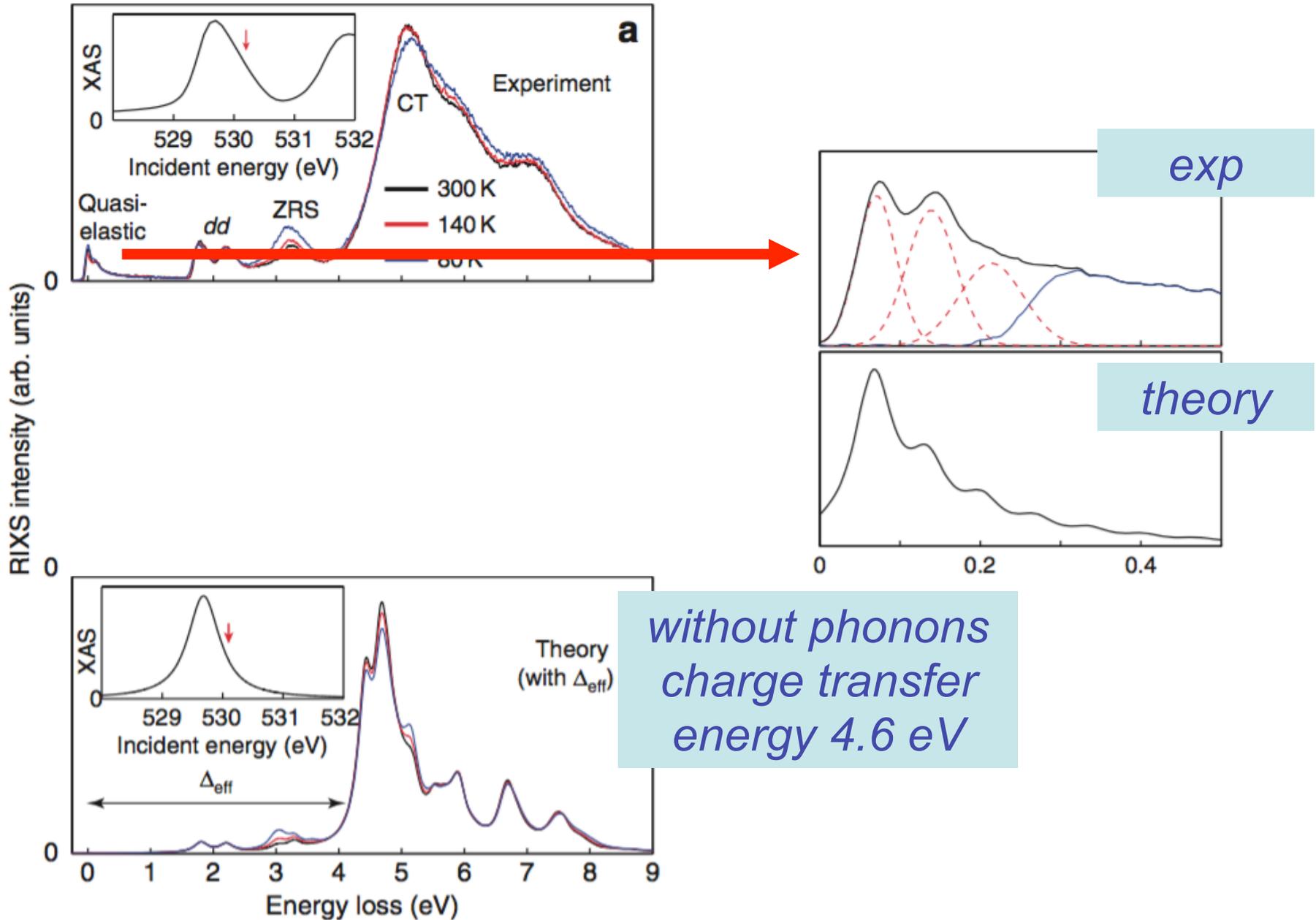


RIXS on Li_2CuO_2

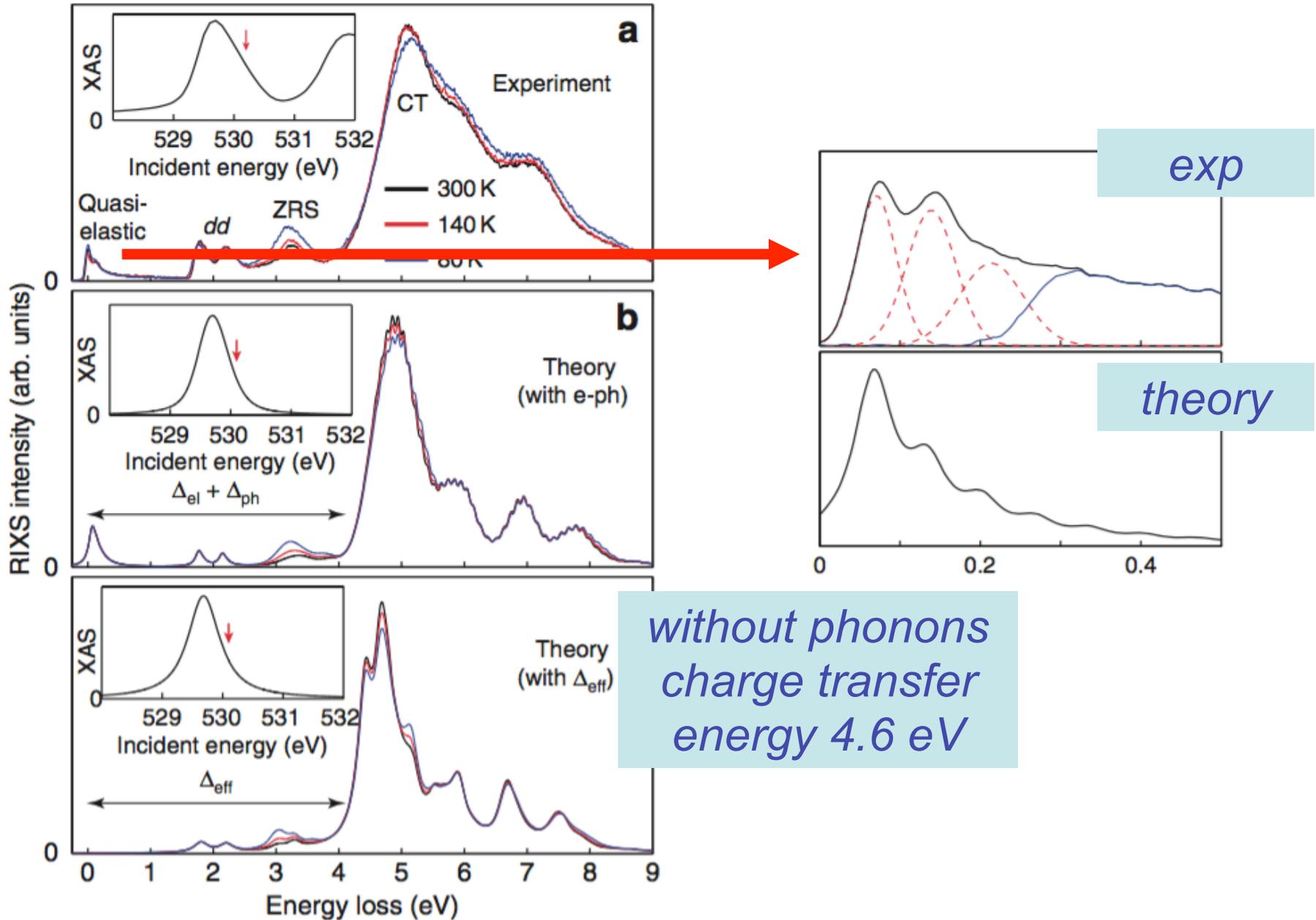


*without phonons
charge transfer
energy 4.6 eV*

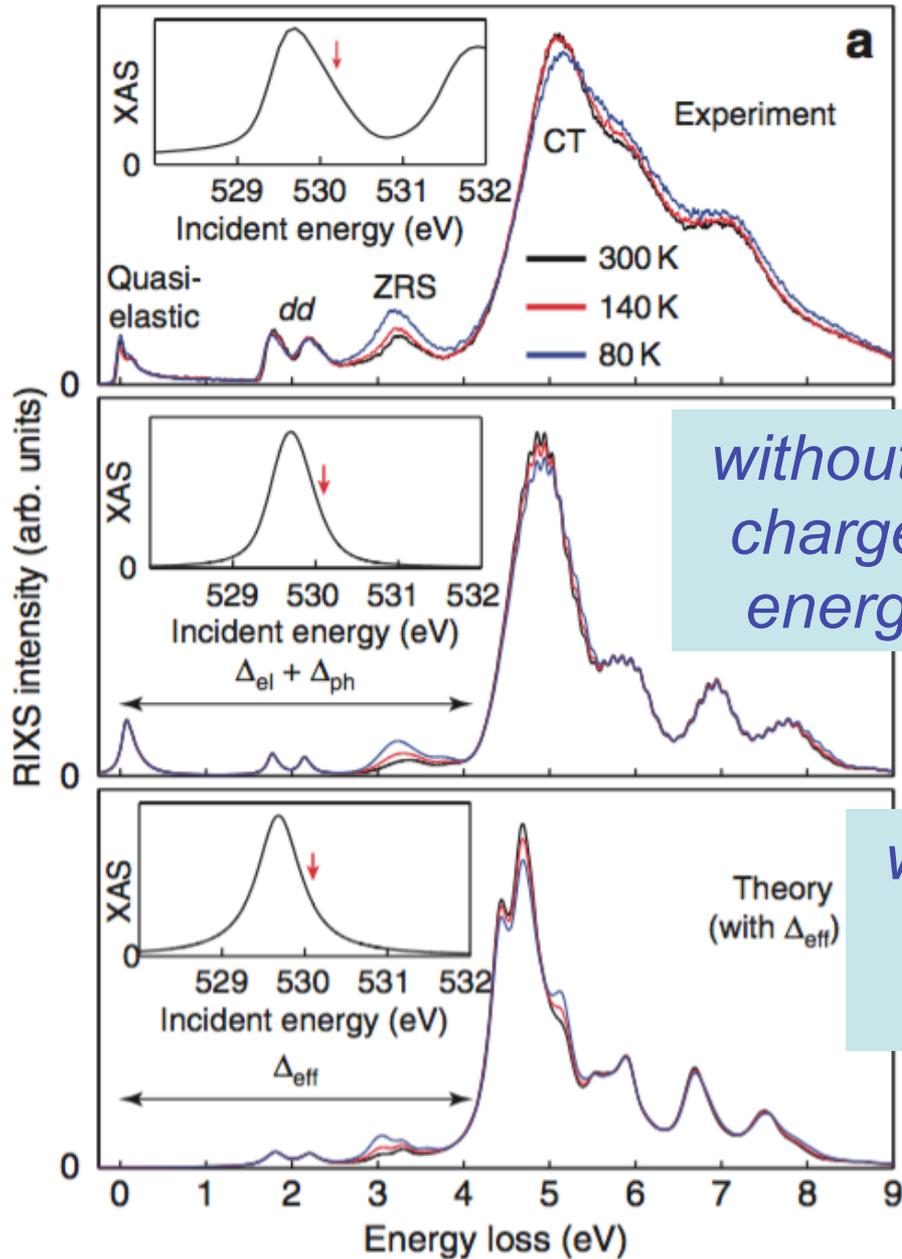
RIXS on Li_2CuO_2



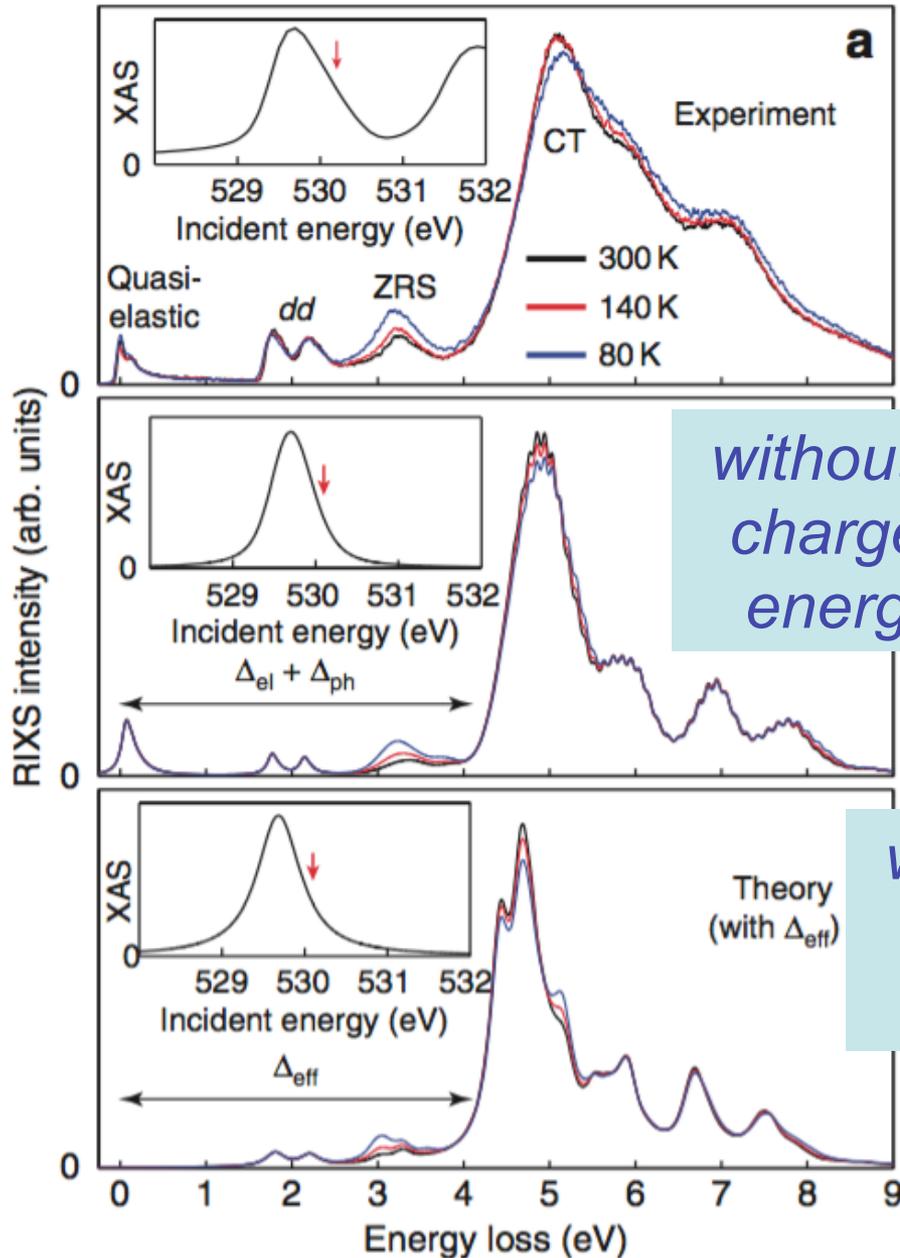
RIXS on Li_2CuO_2



RIXS on Li_2CuO_2



RIXS on Li_2CuO_2

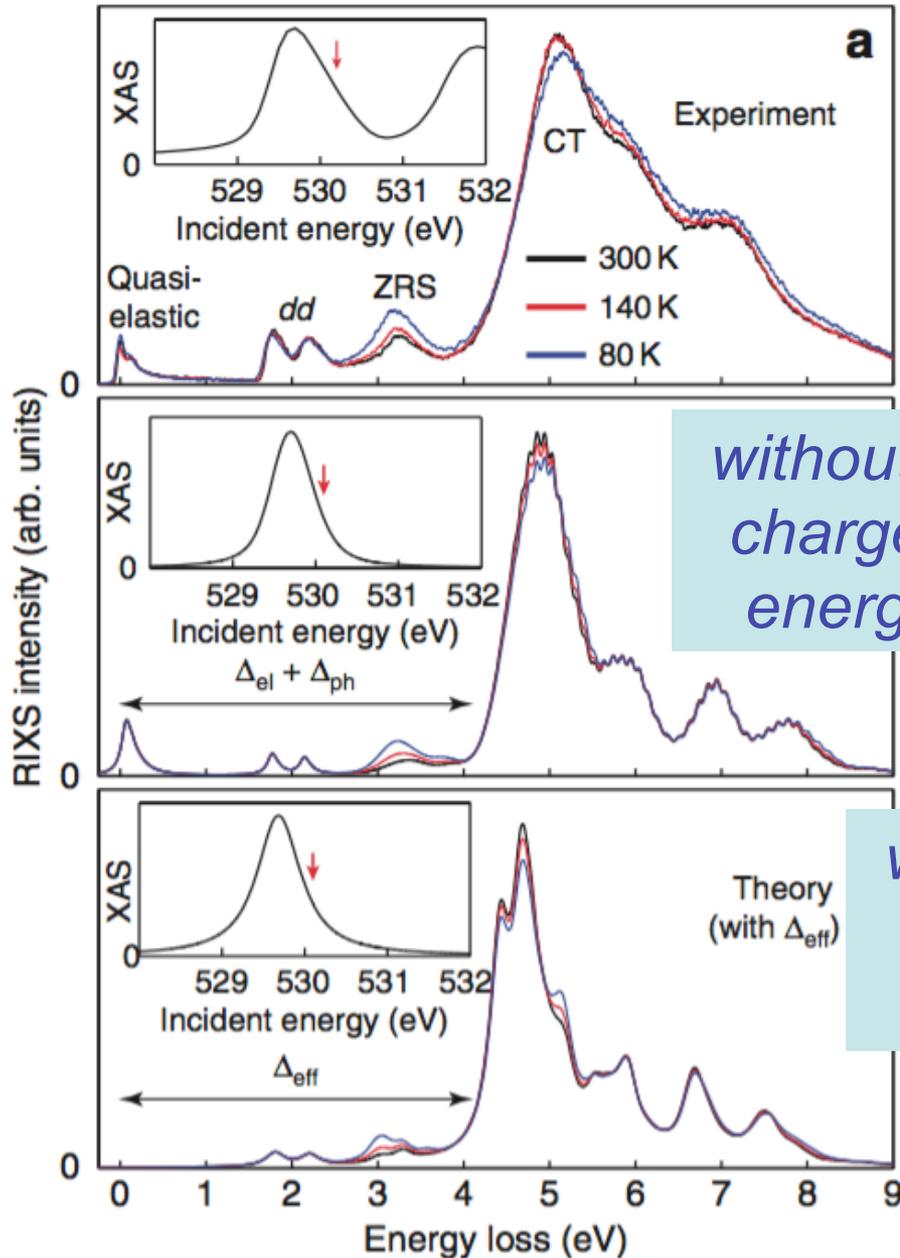


*without phonons
charge transfer
energy 2.1 eV*

*phonon contribution
to “charge transfer”
energy 2.5 eV*

*without phonons
charge transfer
energy 4.6 eV*

RIXS on Li_2CuO_2



phonon induced anti-screening of the CT energy

without phonons charge transfer energy 2.1 eV

phonon contribution to "charge transfer" energy 2.5 eV

without phonons charge transfer energy 4.6 eV

*avoid using dielectric screening for short
(zero)-range coulomb interactions in
correlated electron systems*

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*calculate instead local field induced lattice
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screens Hubbard U

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important differences for nano-structures, at interfaces, at short distances

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depending on lattice nearest neighbor V can be either over or under screened

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dynamic screening very different for electronic and lattice polarizabilities

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**The Hubbard model with orbital degeneracy
and in polarizable media**

Proefschrift

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**The Hubbard model with orbital degeneracy
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Proefschrift

[http://www.rug.nl/research/portal/publications/
pub\(5b75b5ad-8a1b-4ddb-92f9-f73ba8d52479\).html](http://www.rug.nl/research/portal/publications/pub(5b75b5ad-8a1b-4ddb-92f9-f73ba8d52479).html)

RIXS on Li_2CuO_2

